

Piezoelectricity

- Polarization does not disappear when the electric field removed.
- The direction of polarization is reversible.

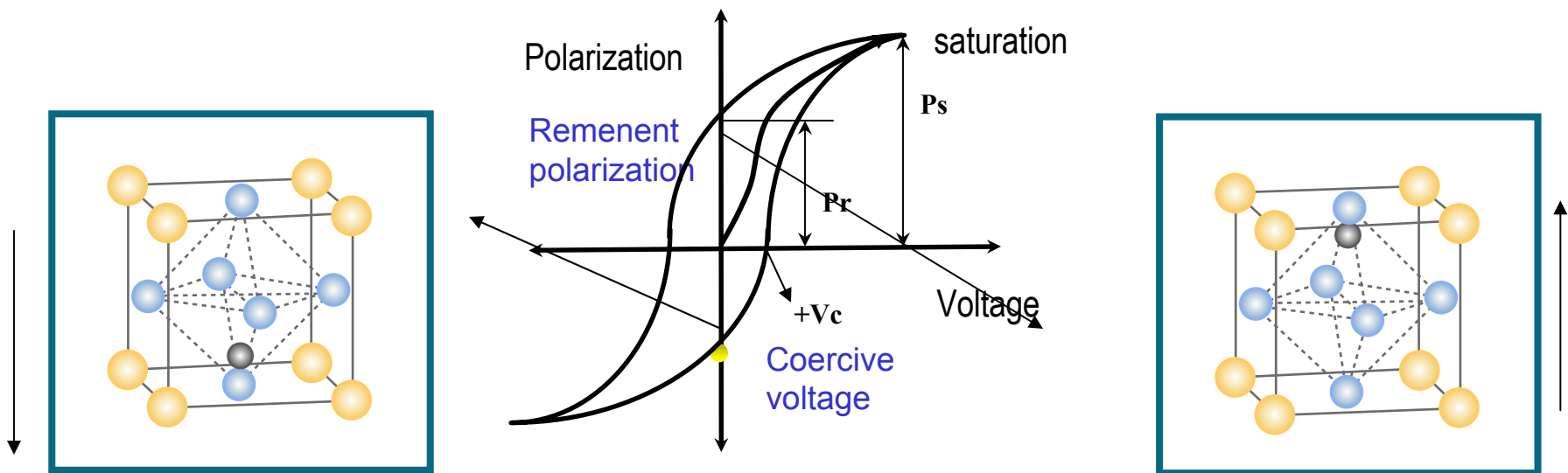
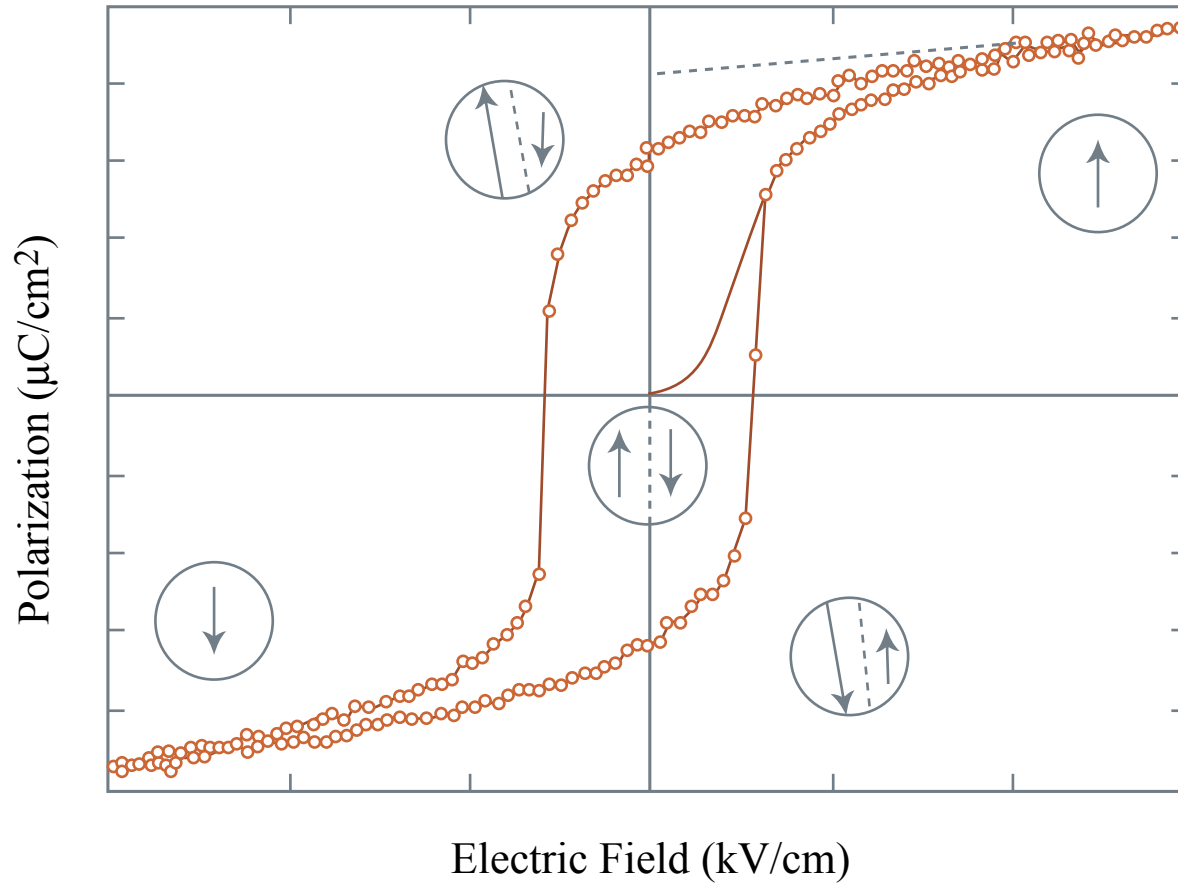


Figure by MIT OCW

FRAM utilize two stable positions.

Figure by MIT OCW

Hysteresis



Ferroelectric (P-E) hysteresis loop. The circles with arrows indicate the polarization state of the material for different fields.

Domain Polarization

- Poling: 100 C, 60kV/cm, PZT
- Breakdown: 600kV/cm, PZT
- Unimorph cantilever

Piezoelectricity

Direct effect

$$D = Q/A = dT$$

Converse effect

$$S = dE$$

$$E = -gT$$

$$T = -eE$$

$$g = d/\epsilon = d/K\epsilon_0$$

$$E = -hS$$

- D: dielectric displacement, electric flux density/unit area
- T: stress, S: strain, E: electric field
- d: Piezoelectric constant, [Coulomb/Newton]

Boundary
Conditions

Free \longrightarrow T

$$d = (\partial S / \partial E)_T = (\partial D / \partial T)_E$$

Short circuit \rightarrow E

$$g = (-\partial E / \partial T)_D = (\partial S / \partial D)_T$$

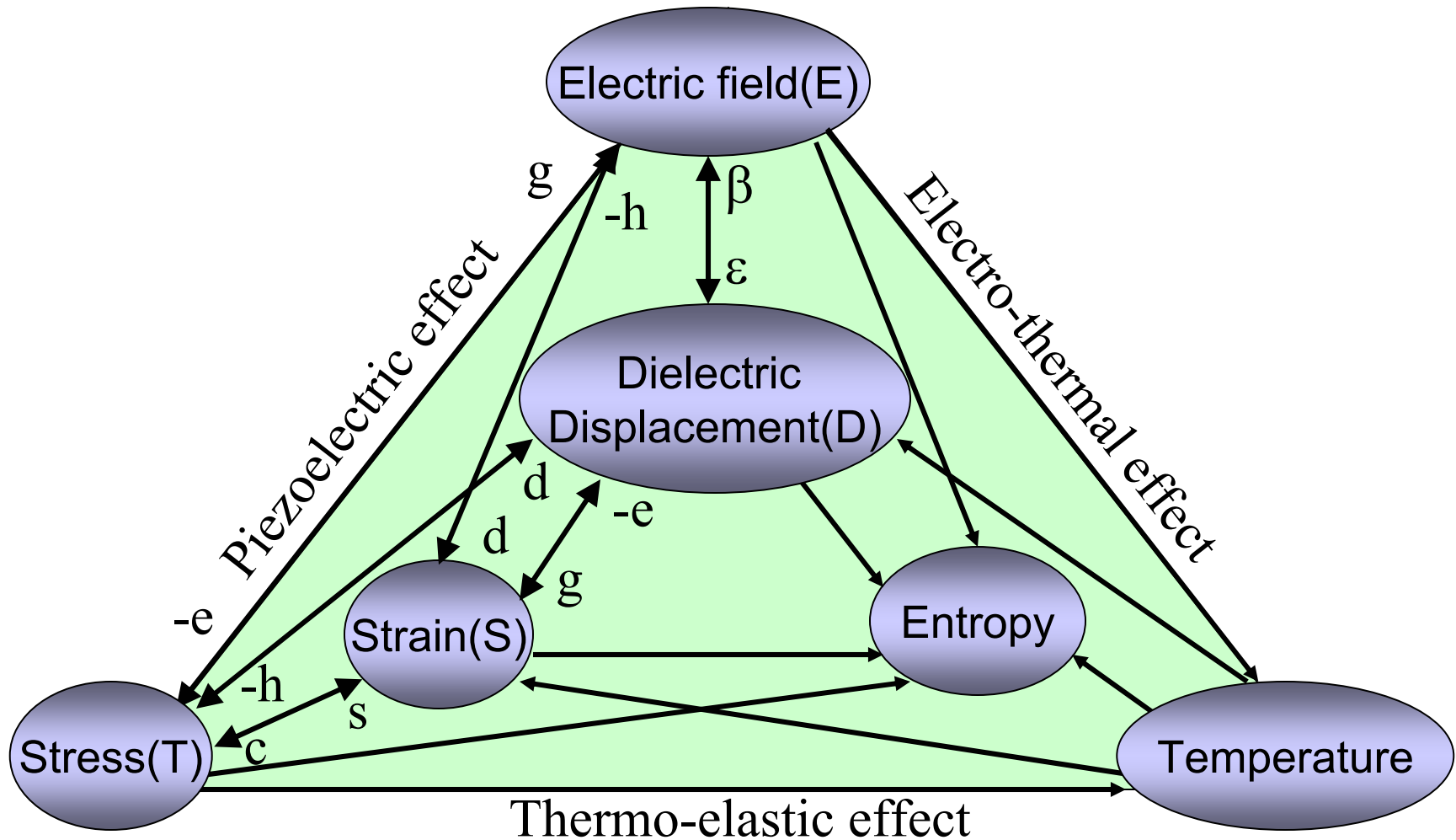
Open circuit \rightarrow D

$$e = (-\partial T / \partial E)_S = (\partial D / \partial S)_E$$

Clamped \longrightarrow S

$$h = (-\partial T / \partial D)_S = (-\partial E / \partial S)_D$$

Principles of piezoelectric



Equation of State

Basic equation

d-form $S_{ij} = s_{ijkl} {}^E T_{kl} + d_{kij} E_k$

$$D_i = d_{ikl} T_{kl} + \varepsilon_{ik} {}^T E_k$$

g-form $S = s^D T + g D$

$$E = -g T + \beta^T D$$

e-form $T_{ij} = c_{ijkl} {}^E S_{kl} - e_{kij} E_k$

$$D_i = e_{kij} S_{kl} + \varepsilon_{ik} {}^S E_k$$

h-form $T = c^D S - h D$

$$E = -h S + \beta^S D$$

$$c^E = 1/s^E$$

$$e = d c^E$$

$$\varepsilon^E = \varepsilon^T - d c^E d_t$$

$$\beta^T = 1/\varepsilon^T$$

$$g = d/\varepsilon^T$$

$$s^D = s^E - d_t (\varepsilon^T)^{-1} d$$

$$D = Q/A$$

$$S = F/A$$

Equation of states

$$\mathbf{D} = \mathbf{d}\mathbf{T} + \boldsymbol{\varepsilon}^T \mathbf{E}$$

direct

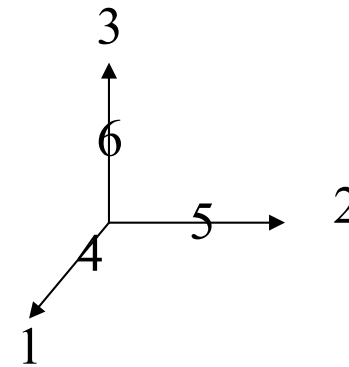
$$\mathbf{S} = \mathbf{s}^E \mathbf{T} + \mathbf{d}\mathbf{E}$$

converse

Tensor to Matrix notation

For cylindrical symmetry, and poling in axis 3,

$$\begin{aligned} D_1 &= \varepsilon_1 E_1 + d_{15} T_5 \\ D_2 &= \varepsilon_1 E_2 + d_{15} T_4 \\ D_3 &= \varepsilon_3 E_3 + d_{31} (T_1 + T_2) + d_{33} T_3 \\ S_1 &= s_{11} T_1 + s_{12} T_2 + s_{13} T_3 + d_{31} E_3 \\ S_2 &= s_{11} T_2 + s_{12} T_1 + s_{13} T_3 + d_{31} E_3 \\ S_3 &= s_{13} (T_1 + T_2) + s_{33} T_3 + d_{33} E_3 \\ S_4 &= s_{44} T_4 + d_{15} E_2 \\ S_5 &= s_{44} T_5 + d_{15} E_1 \\ S_6 &= s_{66} T_6 \end{aligned}$$



Applications of piezoelectric

Sensors

Pressure sensors
Accelerometers
Gyroscopes
Power generators

Actuators

Vibrators
Ultrasonic transducers
Resonators / Filters / Switches
Surface Acoustic wave(SAW) devices
Transformers
Actuators
Ultrasonic motors

Piezoelectric Charge Constants

Electrical energy

Actuator

Mechanical energy

Longitudinal (d_{33})

Diagram removed for copyright reasons.
Source: Piezo Systems, Inc.
"Introduction to Piezo Transducers."
<http://www.piezo.com/bendedu.html>

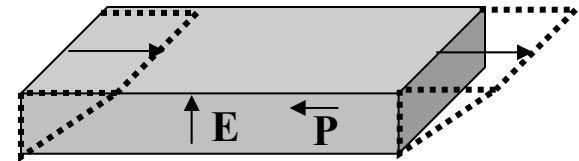
$$\Delta T/T = d_{33} \cdot E$$

Transverse (d_{31})

Diagram removed for copyright reasons.
Source: Piezo Systems, Inc.
"Introduction to Piezo Transducers."
<http://www.piezo.com/bendedu.html>

$$\Delta L/L = d_{31} \cdot E$$

Shear (d_{15})



$$\text{Shear strain} = d_{15} E$$

Piezoelectric Charge Constants

Mechanical energy

Sensor

Electrical energy

Longitudinal (d_{33})

Diagram removed for copyright reasons.
Source: Piezo Systems, Inc.
"Introduction to Piezo Transducers."
<http://www.piezo.com/bendedu.html>

$$Q = d_{33} \cdot F_{in}$$
$$V_{out}/T = g_{33} \cdot F_{in} / (L \cdot W)$$

Transverse (d_{31})

Diagram removed for copyright reasons.
Source: Piezo Systems, Inc.
"Introduction to Piezo Transducers."
<http://www.piezo.com/bendedu.html>

$$Q = d_{31} \cdot F_{in}$$
$$V_{out}/T = g_{31} \cdot F_{in} / (T \cdot W)$$

Multi-layer (d_{33})

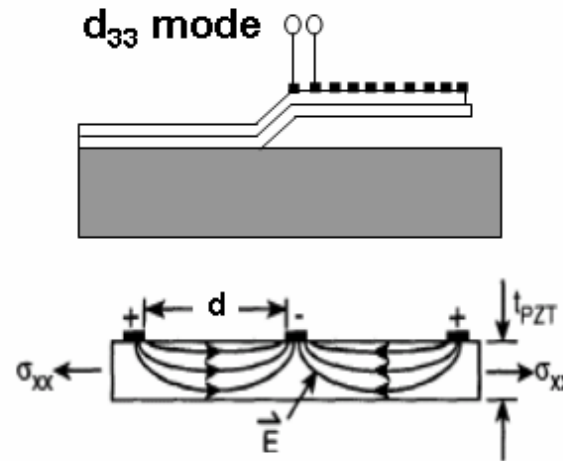
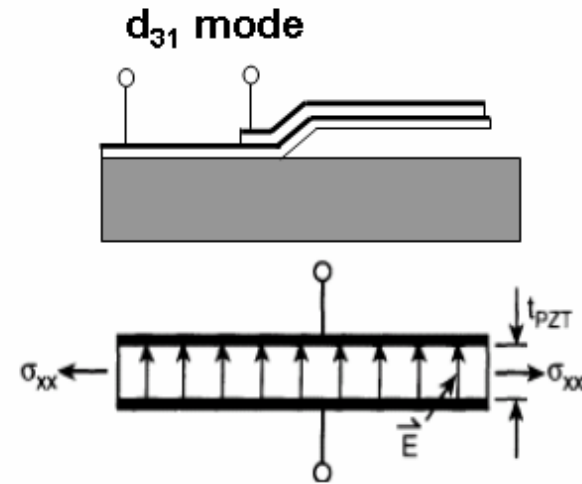
Diagram removed for copyright reasons.
Source: Piezo Systems, Inc.
"Introduction to Piezo Transducers"
<http://www.piezo.com/bendedu.html>

$$Q = n \cdot d_{33} \cdot F_{in}$$
$$V_{out}/T = t/n \cdot g_{33} \cdot F_{in} / (LW)$$

d_{31} vs d_{33}

Homework 2:

Compare generated voltages V_{31} (from d_{31} mode), V_{33} (d_{33} mode). Both have same cantilever dimension, but different electrodes.



$d_{33}=200 \text{ pC/n}$
 $K=1000$

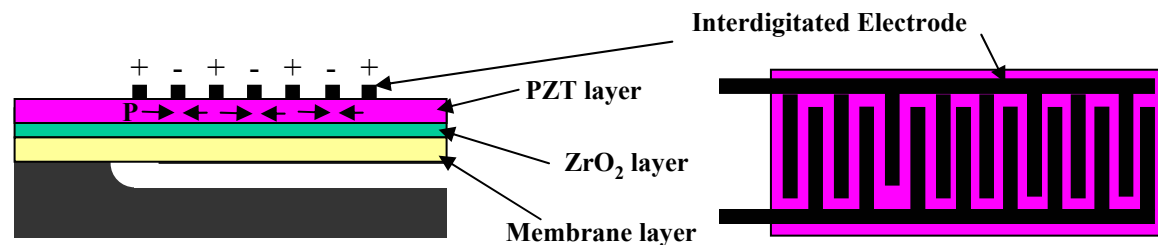
Assume, $g_{33}=2g_{31}$

$t_{pzt}=0.5 \mu$

$d=5 \mu$

length= 100μ , width= 50μ

Young's modulus of the beam= 65 Gpa , max. strain = 0.1%



Design of a Z-positioner

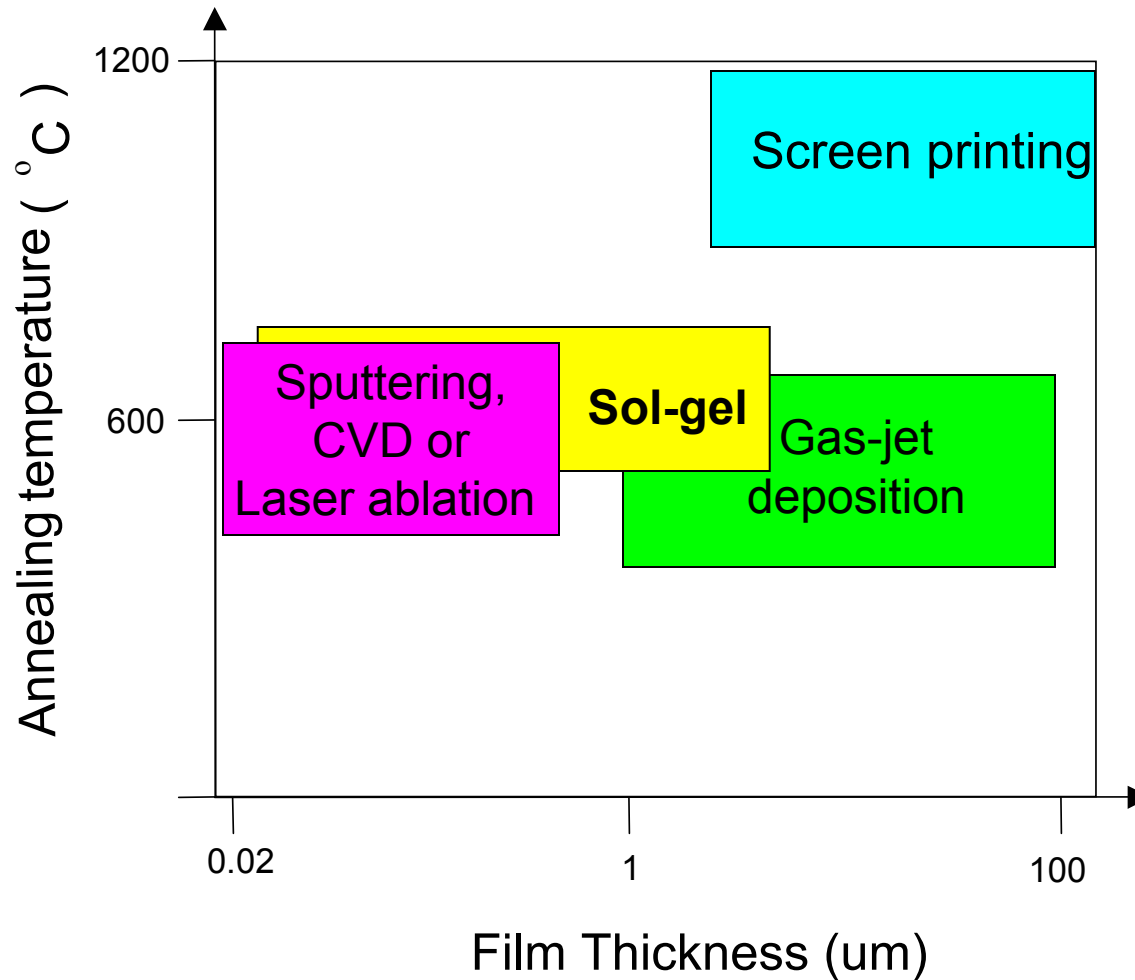
Component schematic removed for copyright reasons.

Physik Instrumente Z-positioner P-882.10, in

http://www.pi-usa.us/pdf/2004_PICatLowRes_www.pdf, page 1-45.

| Ordering Number* | Dimensions A x B x L [mm] | Nominal Displacement [μm @ 100 V] ($\pm 10\%$) | Max. Displacement [μm @ 120 V] ($\pm 10\%$) | Blocking Force [N @ 120 V] | Stiffness [N/ μm] | Electrical Capacitance [μF] ($\pm 20\%$) | Resonant Frequency [kHz] |
|------------------|---------------------------------|---|--|----------------------------------|----------------------------------|---|--------------------------------|
| P-882.10 | 2 x 3 x 9 | 7 | 9 | 215 | 26 | 0.13 | 135 |

Fabrication Methods for PZT thin Films



Sol-Gel spin coating

Advantages

- Vacuum chamber not necessary (simple)
- Easy composition control
- Deposition on large flat substrate

Disadvantages

- Difficult to deposit on deep trenched surface
- Higher raw material consumption

Advantage and disadvantage of PZT film

| Advantage | Disadvantage |
|---|--|
| <p>Unlimited resolution</p> <p>Large force generation</p> <p>Fast expansion</p> <p>No magnetic fields (low cross talk)</p> <p>Low power consumption</p> <p>No wear and tear for actuation</p> <p>Vacuum and clean room compatible</p> <p>Operation at cryogenic temperature</p> | <p>Complex fabrication</p> <p>Hysteresis</p> <p>Life cycle (10^{12} cycles) ; Fatigue, retention...</p> |

Typical Layer Structures for Sol-Gel PZT

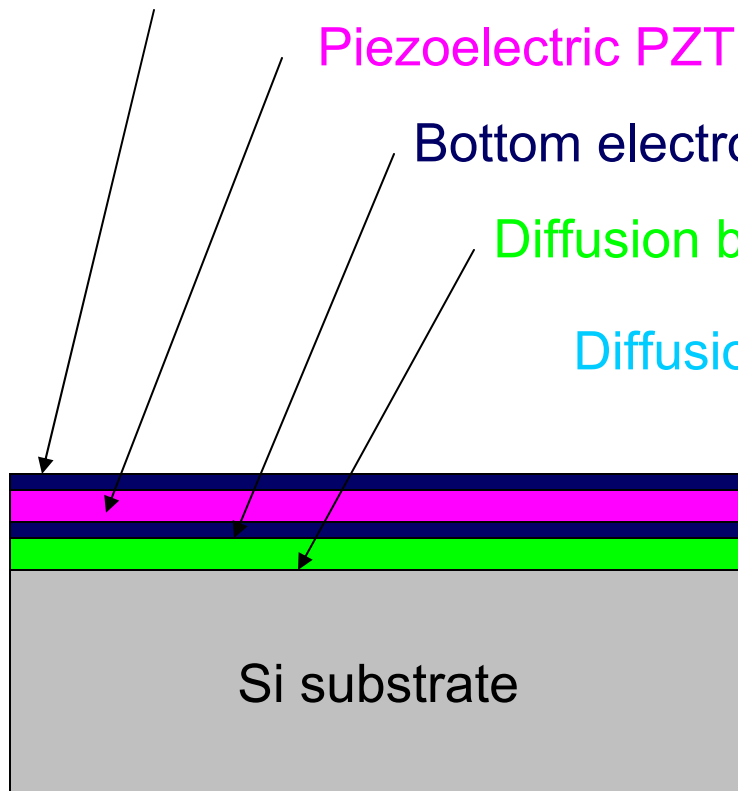
Top electrode Pt (e-beam evaporation lift-off)

Piezoelectric PZT (sol-gel spinning)

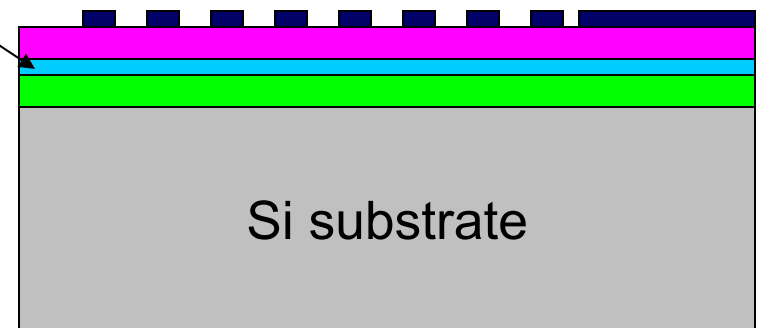
Bottom electrode Pt/Ti (e-beam evaporation lift-off)

Diffusion barrier SiO₂ or SiN_x (CVD)

Diffusion barrier ZrO₂(sol-gel spinning)



d_{31} mode



d_{33} mode

Thermal Oxide Growth and Bottom Electrode Evaporation

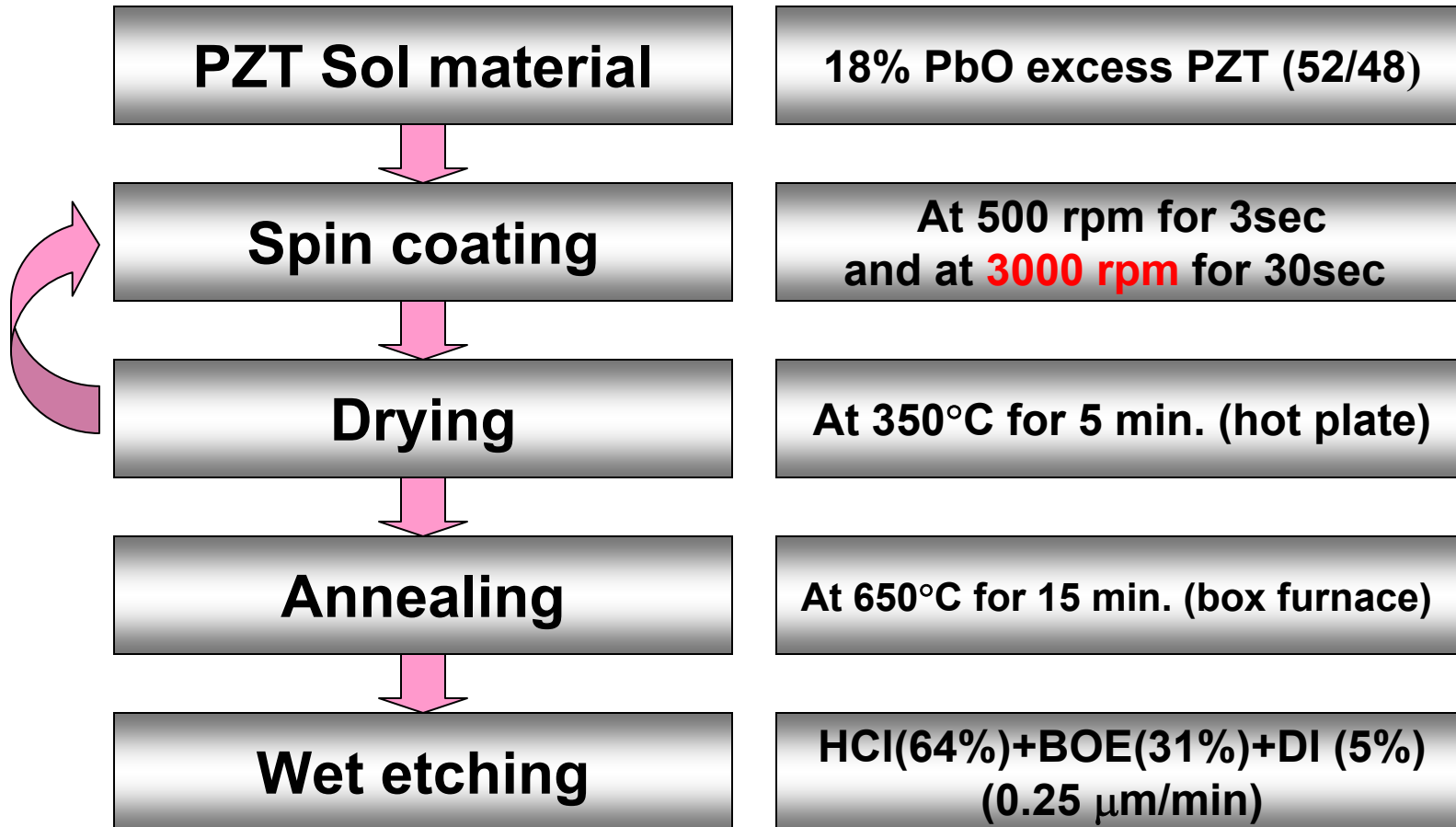


Tubes for growing of device diffusion barrier

Evaporation of device electrodes

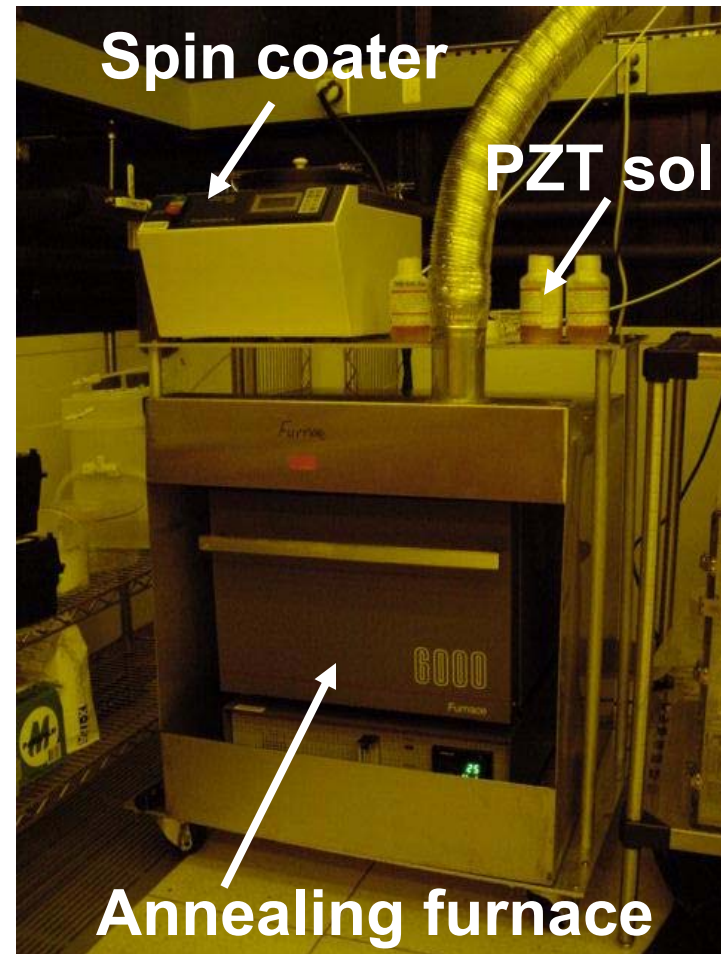
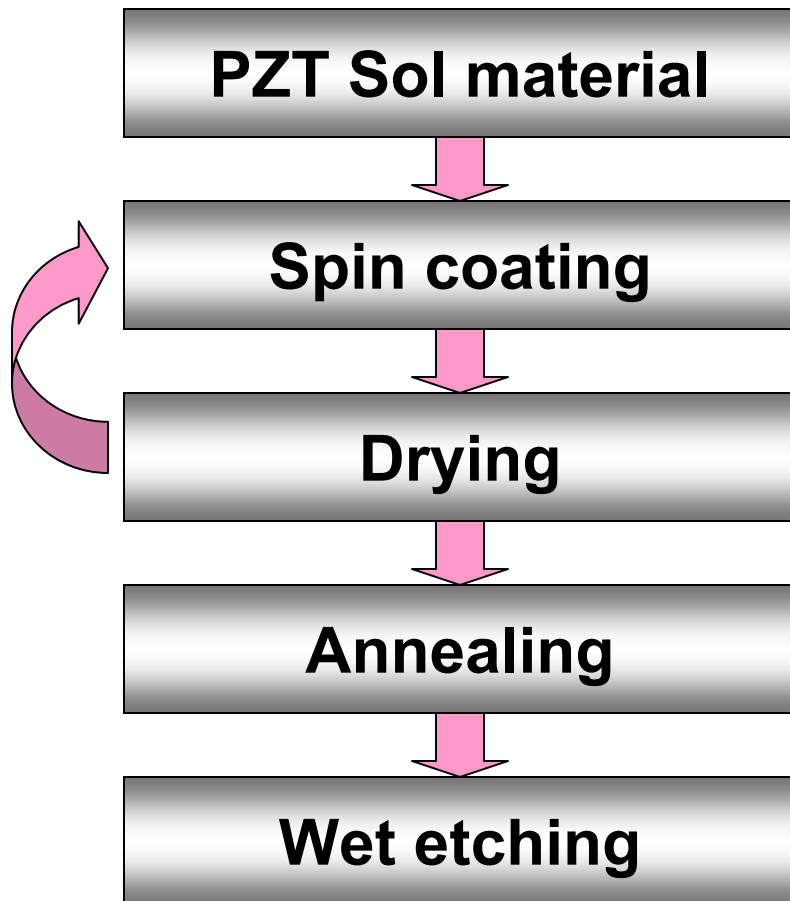


Fabrication of the PZT Film



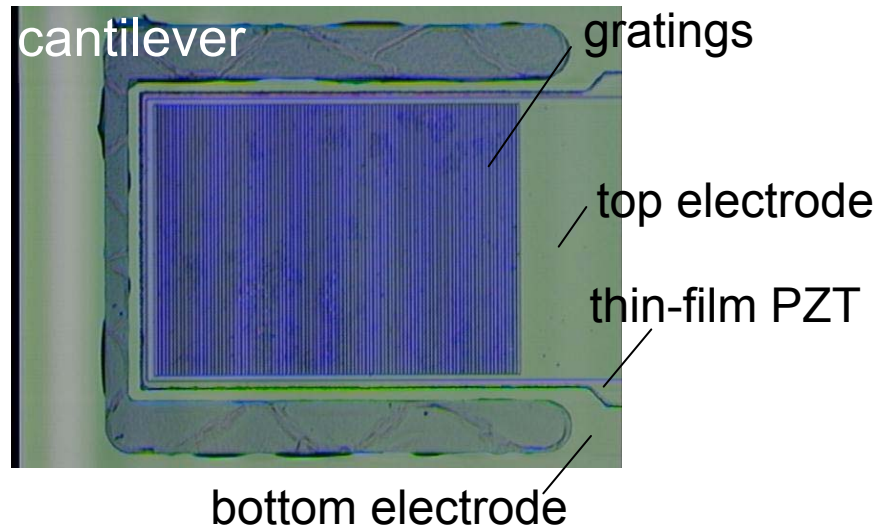
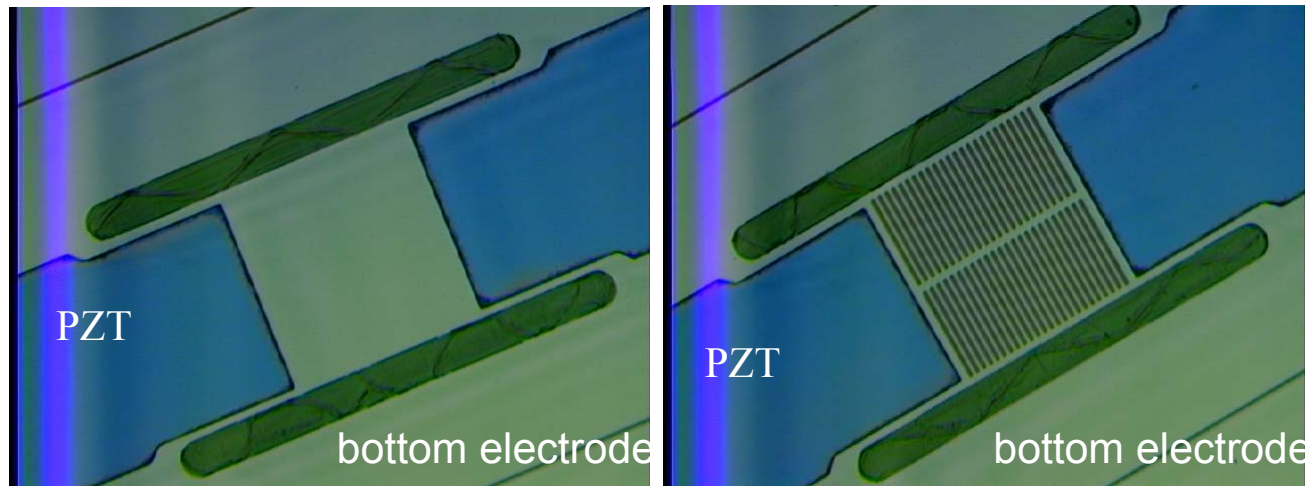
Spin-coat Mitsubishi PZT sol-gel: **15% PZT(118/52/48) A6 Type**

Fabrication of the PZT Film



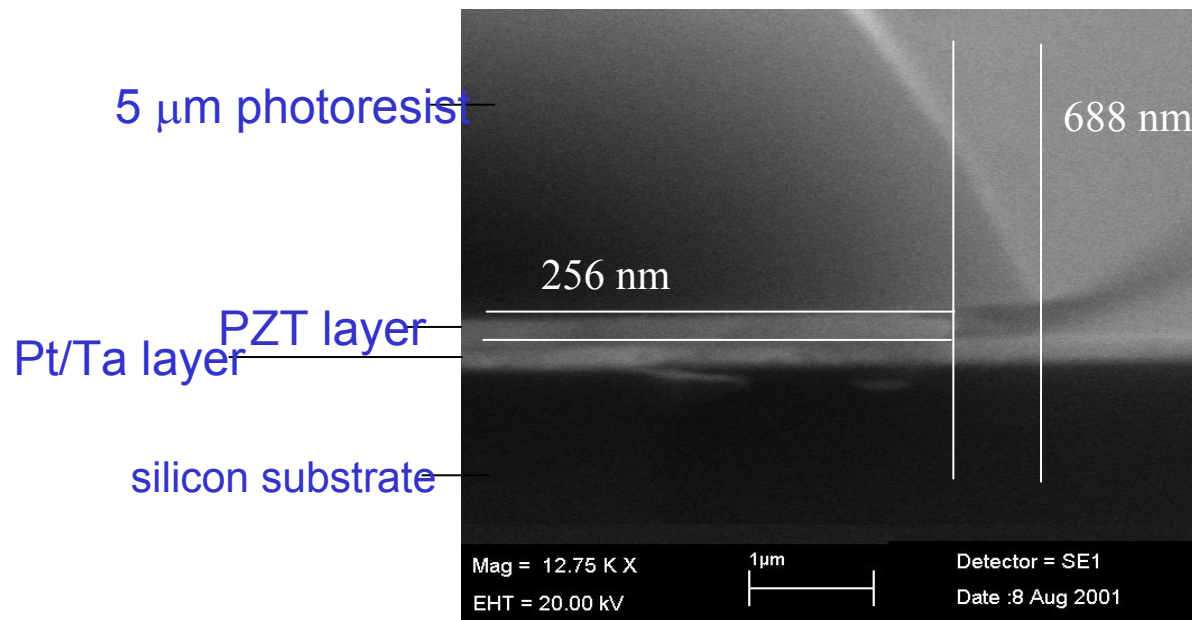
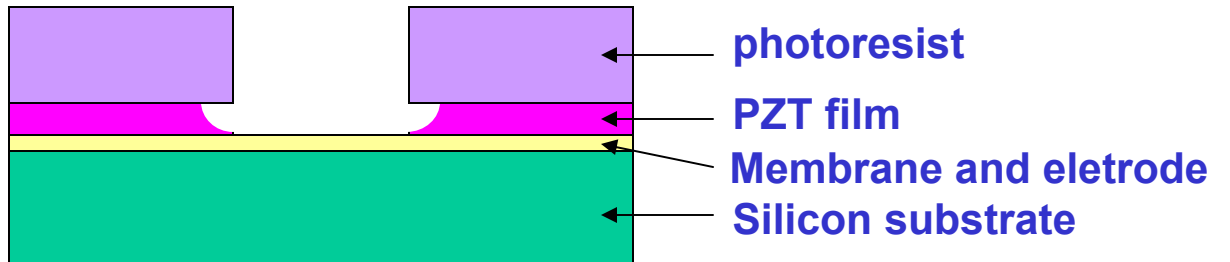
PZT Patterning

Patterned PZT on device



PZT Patterning (Wet etching)

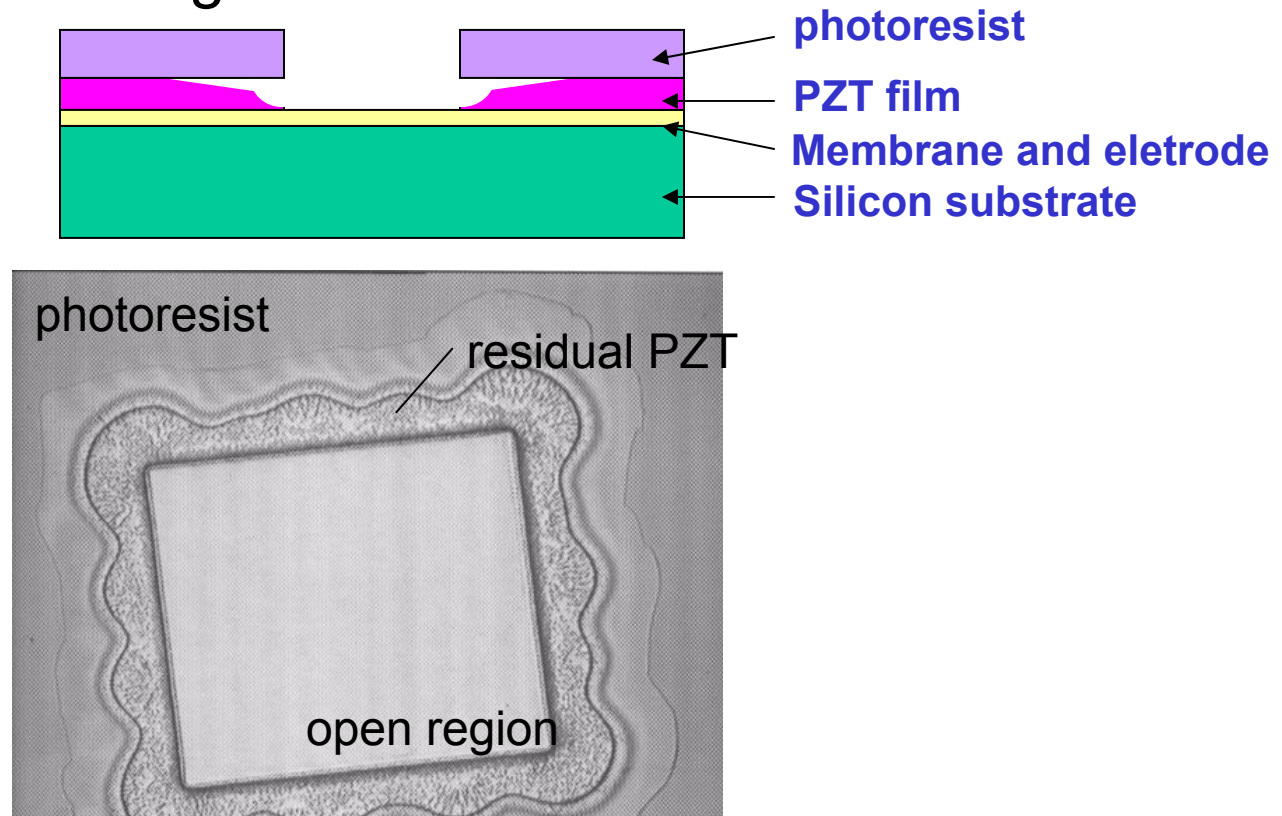
PZT wet-etching with thick photoresist



HCl(64%)+BOE(31%)+DI (5%)
(etch rate: 0.25 μm/min)

PZT Patterning (Wet etching)

PZT wet-etching with thin resist



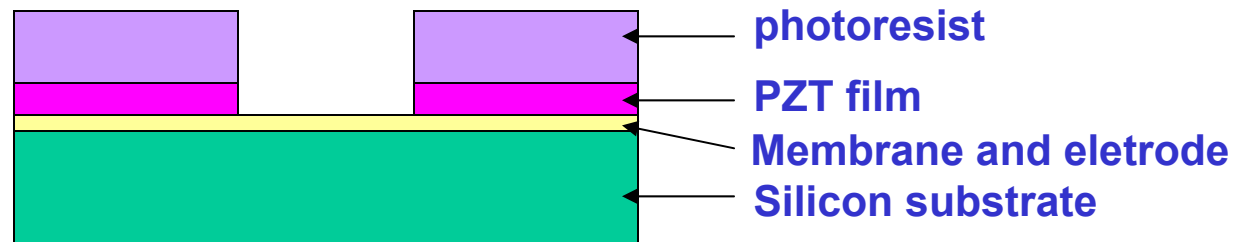
- large undercuts with thin ($1\ \mu\text{m}$) photoresist material

¹ W. Liu *et al*, *Thin Solid Films*, 2000.

² K. Yamashita *et al*, *Transducers '01*, Munich.

PZT Patterning (Dry etching)

PZT dry-etching with thick resist

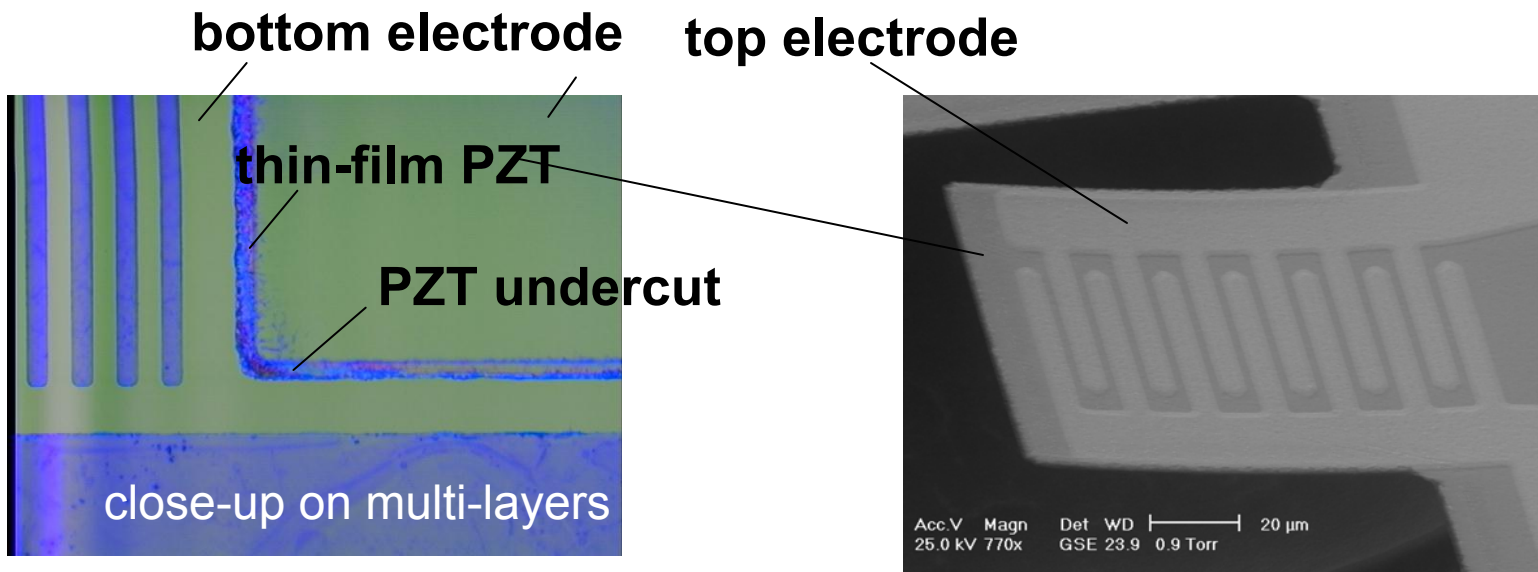


using RIE, Plamaquest (in TRL) or Plasmatherm (in EML)
with $\text{BCl}_3:\text{Cl}_2$ (30:10)

- stiff sidewall with thick ($10\ \mu\text{m}$) photoresist material

Top Electrode Lift-Off

d33 mode interdigitated structure

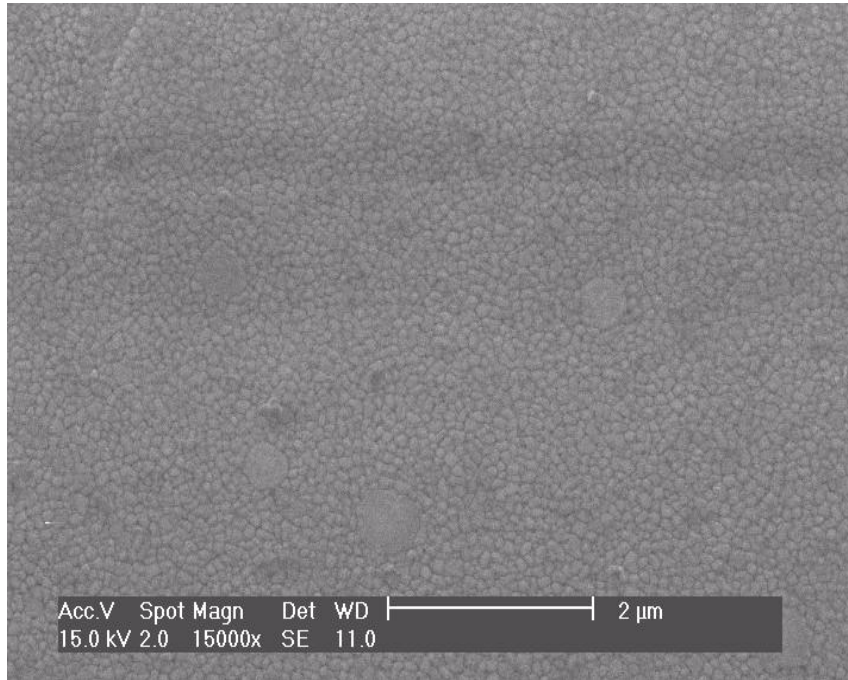


d31 mode sandwich structure

Pt/Ti top electrode pattern by lift-off, 220 nm thick.

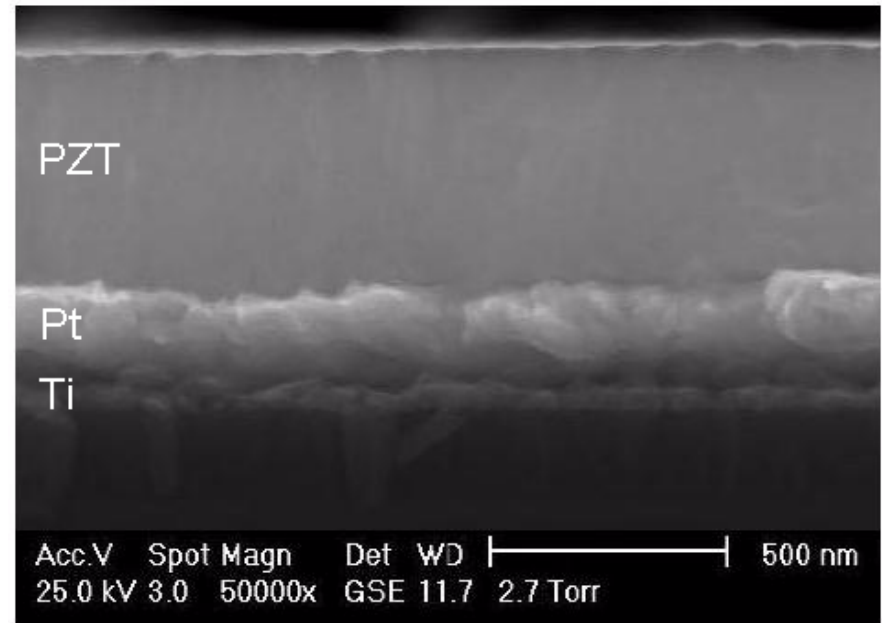
Micro-structure of PZT Thin Film

SEM of PZT film surface



Average grain size : $0.1\mu\text{m}$

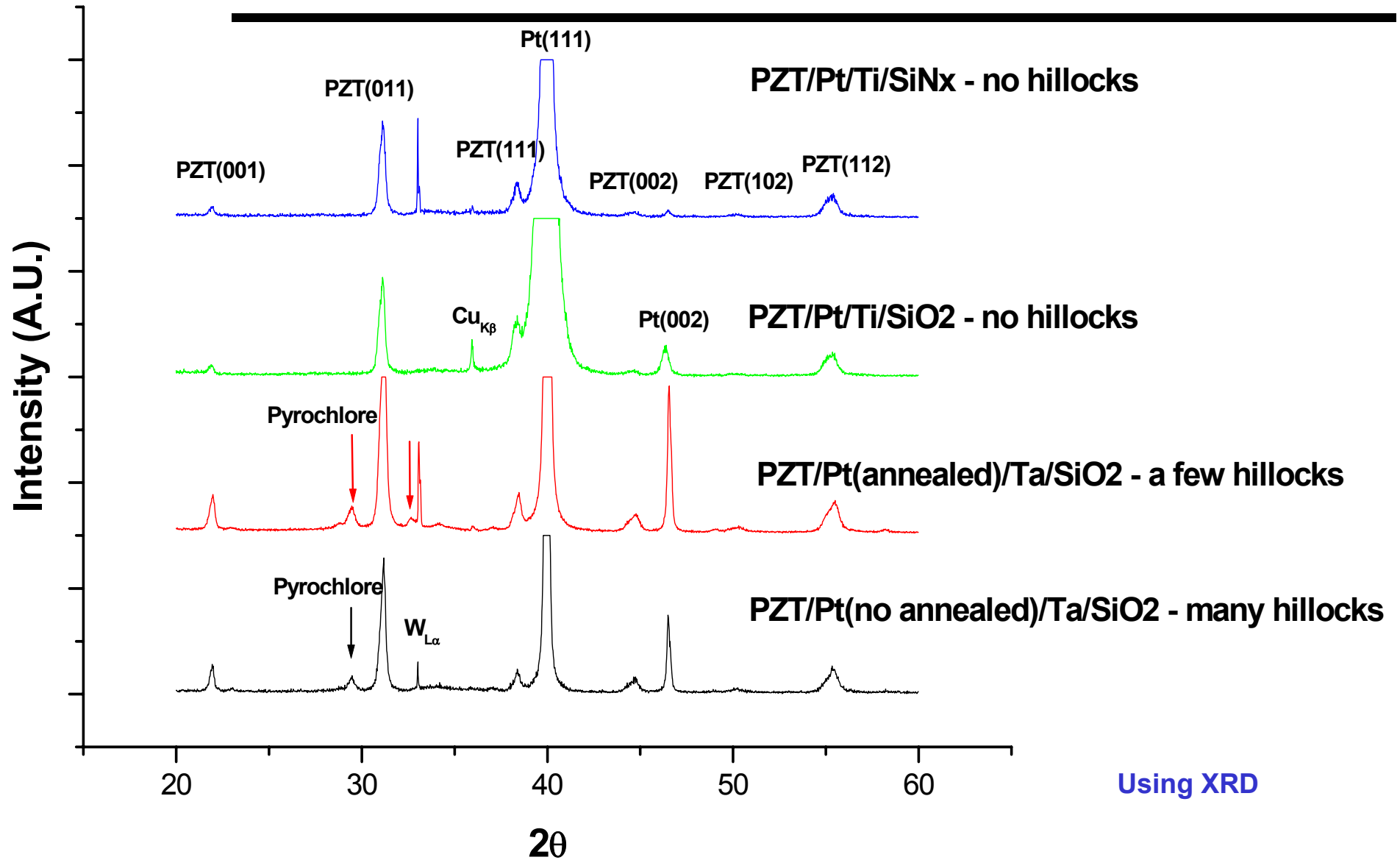
Cross sectional image of PZT film



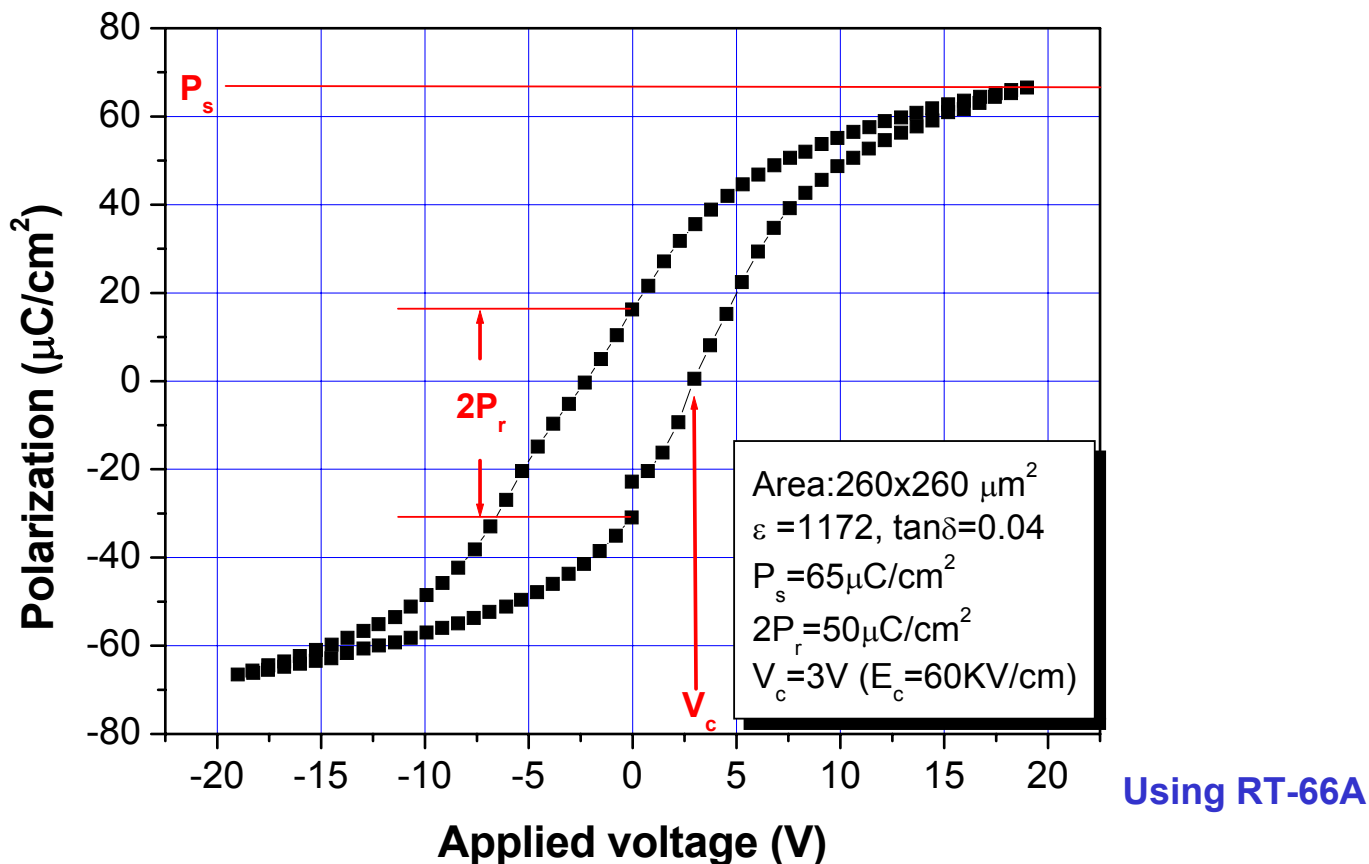
PZT thickness = 510 ± 40 nm;
Pt thickness = 200 nm.

Using SEM

PZT XRD On Various Bottom Electrode Combinations

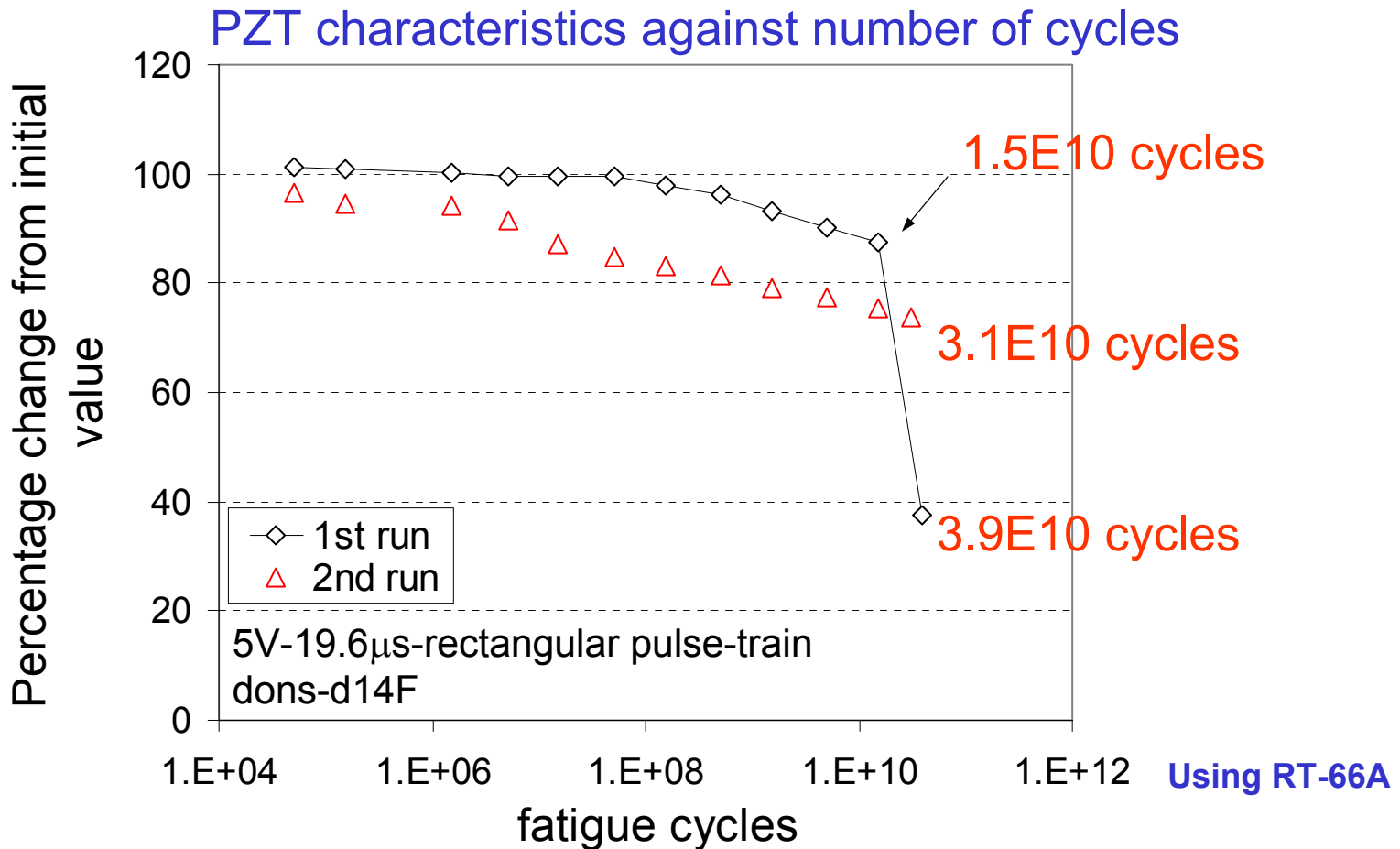


Electrical Measurements - PZT Ferroelectric Characterization



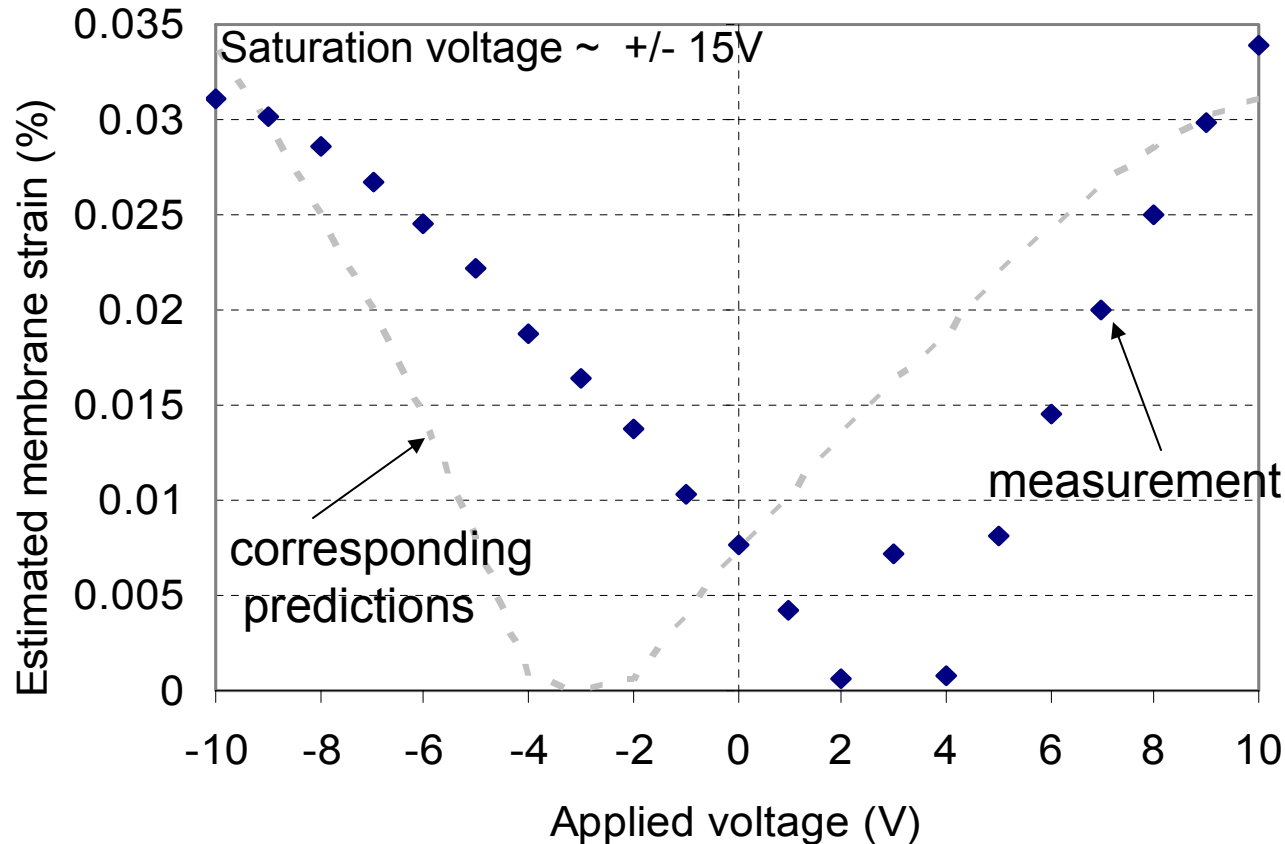
- hysteresis due to domain reorientation - growth, merging and shrinkage
- saturation polarization, P_s at $65 \mu\text{C}/\text{cm}^2$
- remnant polarization, $2P_r$ at $50 \mu\text{C}/\text{cm}^2$

Piezoelectric Fatigue Analysis



- PZT electrical fatigue up to more than 1E10 cycles
- characteristics recovered on 2nd run with same device

Piezoelectric Displacement Analysis



$$\text{strain} = d_{31} V/t$$

$$(d_{33}=275\text{pC/N}^1, d_{31}=-115\text{pC/N}^2)$$

¹ direct measurement

² inferred from mechanical motion