

Code No: 56017

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD

B. Tech III Year II Semester Examinations, November/December - 2015

FINITE ELEMENT METHODS

(Common to ME, AE, MSNT)

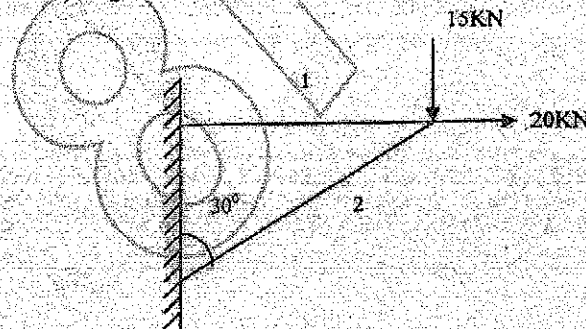
Time: 3 hours

Max. Marks: 75

Answer any five questions

All questions carry equal marks

1. a) State the principle of minimum potential energy.  
 b) Solve the differential equation using Raleigh-Ritz method and Galerkin's method. Compare the solution.  $(d^2\phi / dx^2) + \phi + x = 0$ ,  $0 \leq x \leq 1$  subjected to the boundary conditions  $\phi(0) = \phi(1) = 0$ . [7+8]
2. A stepped bar fixed at both ends rigidly. Starting from left first step of the bar is of 300 mm length, cross sectional area of  $2400 \text{ mm}^2$  and young's modulus is 70 GPa. Second step immediately follows first step and is of length 400 mm, cross sectional area is  $600 \text{ mm}^2$  and young's modulus is 200 GPa. Determine nodal displacement. [15]
3. For the pin jointed truss as shown in the figure. Determine: Element stiffness matrices, Global stiffness matrix, Stresses in the elements 1 and 2, Displacements at all nodes, and Support reactions. Assume  $E = 200 \text{ GPa}$ ,  $L_1 = 750 \text{ mm}$ ,  $L_2 = 900 \text{ mm}$ ,  $A_1 = 100 \text{ mm}^2$ ,  $A_2 = 1250 \text{ mm}^2$ . [15]



Figure

4. Derive shear force and bending moment relations for beam element. [15]
5. A triangular element is specified with the nodal coordinates 1(1, 1), 2(5, 2), 3(3, 6), for a point 'P' located inside the triangle. The shape functions  $N_1$  and  $N_3$  are 0.2 and 0.45, respectively. Determine:  
 a) The x, y coordinates of the point P.  
 b) Determine the shape function  $N_1, N_2, N_3$  at a point Q (3,3). [15]  
 c) Determine the Jacobian matrix.
6. Derive the shape functions for the following:  
 a) 6 noded triangular element.  
 b) 8 noded quadrilateral element.  
 c) 4 noded isoparametric quadrilateral element. [15]

7. A composite slab consists of 3 materials of different conductivities i.e. 20W/m K, 30 W/m K, 50 W/m K of thickness 0.3 m, 0.15 m and 0.15 m, respectively. The outer surface is 20° C and the inner surface is exposed to the convective heat transfer coefficient of 25 W/m<sup>2</sup> K, 800°C. Determine the temperature distribution within the wall. [15]

8. Write short notes about the following.

a) Skyline assembly

b) Higher order elements

c) Eigen values and eigen vectors.

[5+5+5]

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