Code No: 09A30201

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY, HYDERABAD B.Tech II Year I Semester Examinations, November/December-2013 Mathematics-III

(Common to EEE, ECE, EIE, ETM, ECOMPE, ACE)

Time: 3 hours

Max. Marks: 75

Answer any five questions All questions carry equal marks

1.a) Evaluate $\int_{0}^{1} x^{4} \left(\log \frac{1}{x} \right)^{3} dx.$

b) State and prove generating function for $J_n(x)$.

[15]

2.a) Prove that $(2n+1) P_n(x) = P_{n+1}^1(x) - P_{n-1}^1(x)$.

b) Prove that $\int_{-1}^{1} x P_n(x) P_{n-1}(x) dx = \frac{2n}{4n^2 - 1}$. [15]

3.a) Show that the function $f(x) = \begin{cases} \frac{x^3 y(y - ix)}{x^6 + y^2}, z \neq 0 \\ 0, z = 0 \end{cases}$ is not differentiable at the origin.

b) Find all the roots of Sin z = 2.

[15]

4.a) Evaluate $\int_{0}^{1+i} (x^2 + iy) dz$ along the path y = x and $y = x^2$.

b) Use Cauchy's Integral formula to evaluate $\int_C \frac{z-1}{(z+1)^2(z-2)} dz$, where 'C' is the circle |z-i|=2.

5.a) Find the Taylor's series expansion of e^z about z = 3.

b) Expand
$$f(z) = \frac{z^2 - 4}{z^2 + 5z + 4}$$
 in the region $1 < |z| < 4$. [15]

6.a) Evaluate $\int_C \frac{4-3z}{z(z-1)(z-2)} dz$, where 'C' is the circle $|z| = \frac{3}{2}$ using Residue theorem.

b) Evaluate by contour Integration
$$\int_{0}^{\infty} \frac{dx}{1 + \dot{x}^{2}}.$$
 [15]

7.a) Show that the function $w = \frac{4}{z}$ transforms the straight line x=c in the z-plane in to a circle in the w-plane.

b) Under the transformation $w = \frac{z - i}{1 - iz}$ find the image of the circle

(i)
$$|w| = 1$$

(ii) |z| = 1 in the w-plane.

[15]

8.a) Draw the undirected graph represented by the adjacency matrix A given below.

$$A = \begin{bmatrix} 1 & 2 & 0 & 0 \\ 3 & 0 & 1 & 1 \\ 0 & 1 & 2 & 2 \\ 0 & 1 & 2 & 0 \end{bmatrix}$$

b) Suppose all vertices in a graph have odd degree 'K' Show that total number of edges in G is multiple of K. [15]

