

B.Tech II Year - II Semester Examinations, April-May, 2012

CONTROL SYSTEMS

(COMMON TO ELECTRONICS AND INSTRUMENTATION ENGINEERING,
INSTRUMENTATION AND CONTROL ENGINEERING)

Time: 3 hours

Max. Marks: 75

Answer any five questions
All questions carry equal marks

- 1.a) Distinguish between open loop and closed loop systems. Explain merits and demerits of open loop and closed loop systems.
- b) Obtain the mathematical model for the system shown in Figure.1. [7+8]

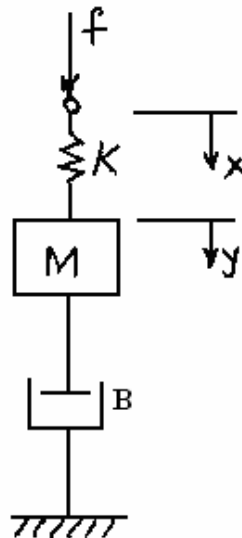


Figure.1

- 2.a) Derive from fundamentals, the transfer function of AC Servo Motor.
- b) Using block diagram reduction techniques, find the closed loop transfer function of the system whose block diagram is given in Figure.2. [7+8]

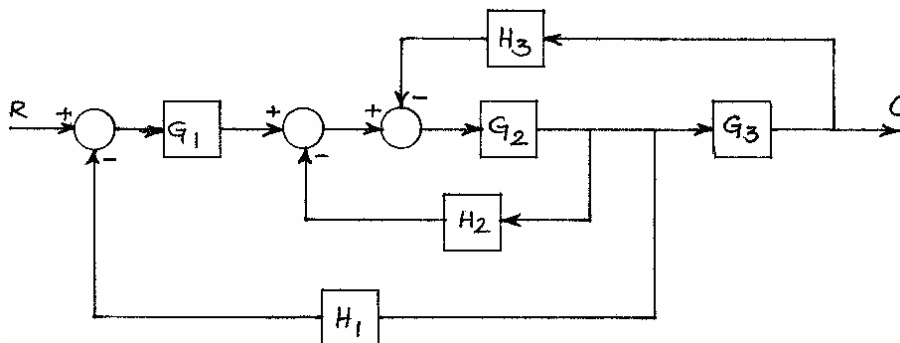


Figure.2

- 3. A unity feedback system has a forward transfer function of $\frac{K}{s^2}$ and a feedback elements transfer function of $(as + b)$. Determine steady-state error, when the input is $r(t) = 1 + t + t^2/2$. Specify the values of K , a and b to limit the steady state error for this input to 0.02. [15]

- 4.a) Construct the root-locus plot for the control system shown in Figure.3.

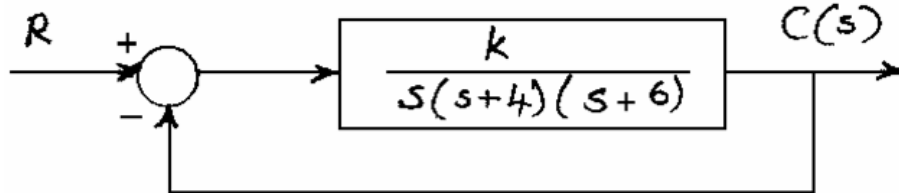


Figure.3

- b) The characteristic equation of a servo system is given by $a_0 s^4 + a_1 s^3 + a_2 s^2 + a_3 s + a_4 = 0$. Determine the conditions which must be satisfied by the coefficients of the characteristic equation for the system to be stable. [15]
- 5.a) Consider the open loop transfer function of the system $G(s) = \frac{3}{s(0.05s+1)(0.2s+1)}$ with unity feed back. Obtain the maximum gain $M_{p\omega}$, resonant frequency ω_r and the band width ω_b of the system.
- b) Explain the procedure to construct the Bode plot. [10+5]
- 6.a) Sketch the polar plot of the transfer function $G(s) = \frac{1}{(1+T_1s)(1+T_2s)(1+T_3s)}$. Determine the frequency at which the polar plot intersects the real and imaginary axis of $G(j\omega)$ plane.
- b) Explain the term relative stability in detail. Also discuss determination of phase and gain margins from Nyquist plot. [8+7]
7. Consider a unity – feedback control system whose feed forward transfer function is given by $G(s) = \frac{10}{s(s+2)(s+8)}$. Design a compensator so that the static velocity error coefficient K_v is equal to 80 sec^{-1} and the dominant closed-loop poles are located at $s = -2 \pm j 2\sqrt{3}$. [15]
- 8.a) A feed back system has a closed loop transfer function. $\frac{Y(s)}{R(s)} = \frac{10}{s(s+1)(s+4)}$. Construct a state variable model for the system.
- b) Consider the homogeneous equation $\dot{X}(t) = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} X(t)$. Find the response $X(t)$ when $X(0) = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$. [7+8]

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- 1.a) For the given lever system shown in Figure.1, determine the equation relating f and x .

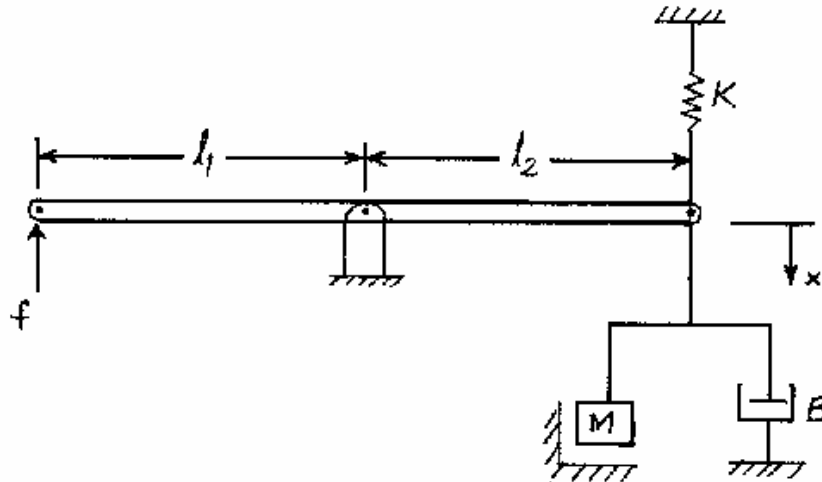


Figure.1

- b) What are the various types of control systems? Give an example of each? What are advantages and disadvantages of open loop and closed loop systems? [8+7]
2. From the block diagram shown in Figure.2, determine $\frac{C_1}{R_1}$ and $\frac{C_2}{R_2}$ by making suitable assumptions. Also verify with signal flow graph technique. [15]

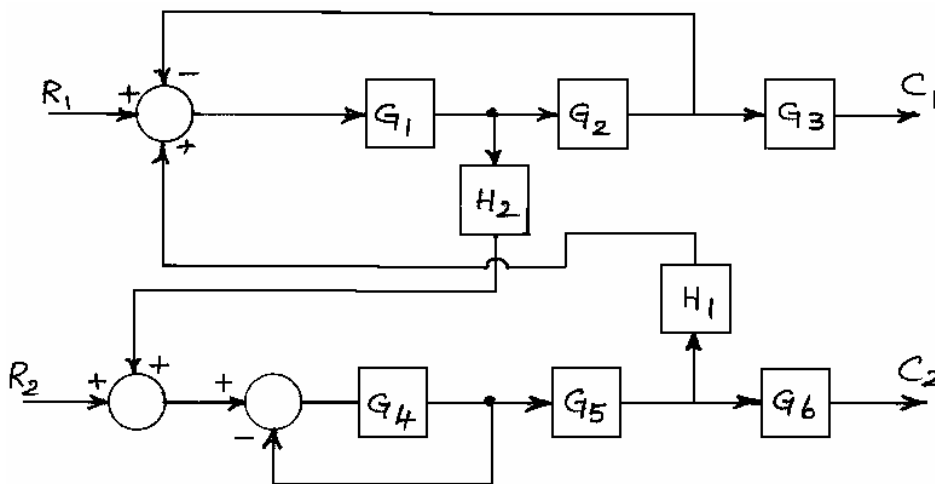


Figure.2

3. The block diagram of a feedback control system is shown in Figure.3 below. It is desired that
- The steady state error due to a unit step function input is zero.
 - The characteristic equation of the overall system is $s^3 + 4s^2 + 6s + 10 = 0$. Find the third order open loop transfer function $G(s)$, so that the above two requirements are satisfied simultaneously. [15]

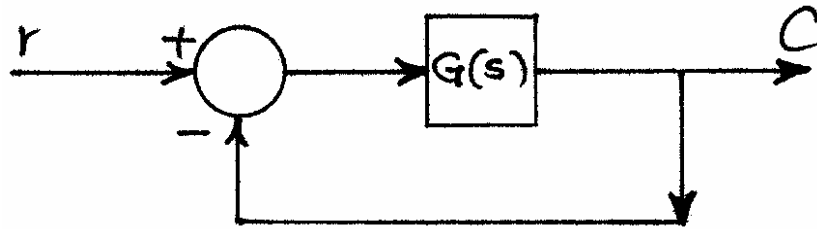


Figure.3

4. A feedback control system has an open-loop transfer function $G(s) H(s) = \frac{K}{s(s+3)(s^2+2s+2)}$. Find the root locus as K is varied from 0 to ∞ . Also find the value of K on imaginary axis if locus crosses imaginary axis. [15]
5. Plot the approximate Bode plot for the transfer function $G(s) = \frac{100(s+3)}{s(s+1)^2 \left(1 + \frac{s}{30}\right)}$. Also find the gain margin and phase margin. [15]
- 6.a) Explain the Nyquist criterion for assessing the stability of a closed loop system.
- b) Sketch the Nyquist plot for the transfer function: $G(s) H(s) = \frac{52}{(s+2)(s^2+2s+5)}$. Discuss its stability. [15]
7. Explain the design considerations of lead and lead-lag compensation based on frequency-response approach. [15]
- 8.a) Obtain the transfer function of the system described by $\dot{X} = \begin{bmatrix} -5.0 & -1.0 \\ 3 & -1.0 \end{bmatrix} X + \begin{bmatrix} 2 \\ 3 \end{bmatrix} u$ and $Y = [1 \ 2] X$.
- b) The state space representation of a system is given by $\dot{X} = \begin{bmatrix} -5.0 & 1 \\ -6 & 0.0 \end{bmatrix} X$. Find the value of $x_1(t)$ at $t=1$, if $x_1(0)$ and $x_2(0) = 0$. [15]

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1.a) Write the system dynamic equations for the given in figure.1 mechanical system

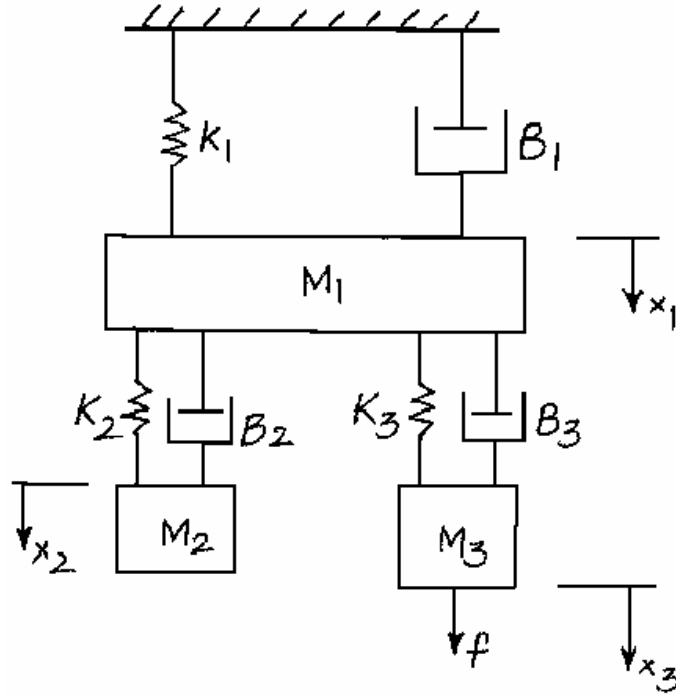


Figure.1

b) Distinguish between open loop and closed loop systems. [10+5]

2. Using block diagram reduction techniques find the closed loop transfer function of the system whose block diagram is given in Figure.2 and verify the result using signal flow graph technique. [15]

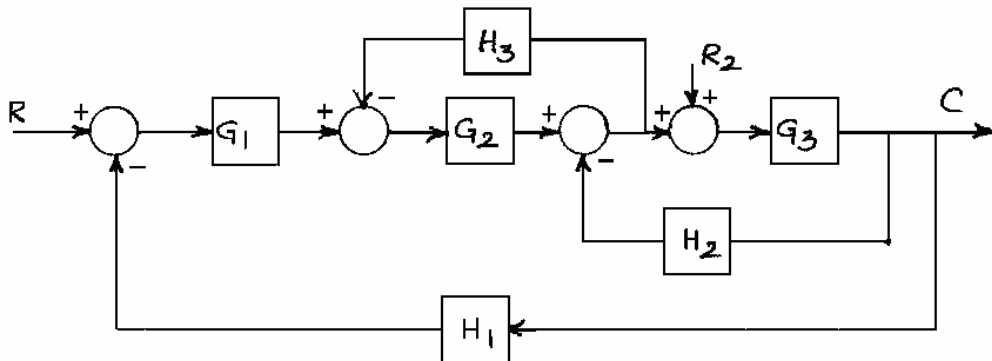


Figure.2

3. A feedback system employing output-rate damping is shown in Figure.3 below:
- In the absence of derivative feedback ($K_o = 0$), determine the damping factor and natural frequency of the system. What is the steady-state error resulting from unit-ramp input?
 - Determine the derivative feedback K_o , which will increase the damping factor of the system to 0.6. What is the steady-state error to unit-ramp input with this setting of the derivative feedback constant?
 - Illustrate how the steady-state error of the system with derivative feedback to unit-ramp input can be reduced to same value as in part (a), While the damping factor is maintained at 0.6. [15]

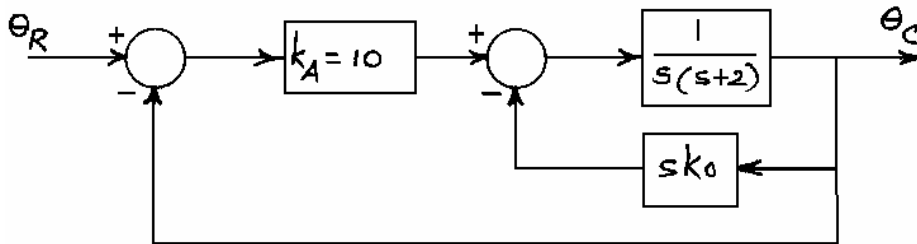


Figure.3

4. The unity feedback control system has an open-loop transfer function $G(s) = \frac{K(1+2s)(1+0.25s)}{s^3(1+0.01s)(1+0.05s)}$. Sketch the root locus diagram. Determine the points of the loci on the $j\omega$ axis and the corresponding values of gain K and frequency ω . [15]
5. Plot the approximate Bode plot for the following transfer function: $G(s) = \frac{11.1(s^2 + 0.1s + 9)}{s\left(1 + \frac{s}{0.1}\right)\left(1 + \frac{s}{10}\right)}$. Also find the gain margin and phase margin. [15]
- 6.a) For the given unity feedback system with: $G(s) = \frac{K(1+0.5s)(s+1)}{(1+10s)(s-1)}$, sketch the Nyquist plot and determine the range of K for which the system is stable.
 b) Explain the phase margin and gain margin with respect to Nyquist criteria. [15]
7. The open loop transfer function of unity feedback system is $G(s) = \frac{k}{s(s+1)}$. It is desired to have the velocity error constant $K_v = 12 \text{ Sec}^{-1}$ and phase margin as 40° . Design lead compensator to meet the above specifications. [15]
- 8.a) What are the advantages of state space representation? Explain.
 b) Obtain the transfer function of the system described by $\dot{X} = \begin{bmatrix} -5.0 & -1.0 \\ 3 & -1.0 \end{bmatrix} X + \begin{bmatrix} 2 \\ 3 \end{bmatrix} u$ and $Y = [1 \ 2] X$.
 c) What are the properties of state transition matrix? Explain. [4+7+4]

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- 1.a) Explain various types of control systems with suitable examples.
b) Explain the effects of feedback in closed loop control systems. [7+8]

- 2.a) Construct the Signal Flow Graph for the given set of equations

$$x_2 = a_{12} x_1 + a_{32} x_3 + a_{42} x_4 + a_{52} x_5$$

$$x_3 = a_{23} x_2$$

$$x_4 = a_{34} x_3 + a_{44} x_4$$

$$x_5 = a_{35} x_3 + a_{45} x_4$$

and obtain the overall transfer function.

- b) Find the closed loop transfer function of the system whose block diagram is given in Figure.1. [7+8]

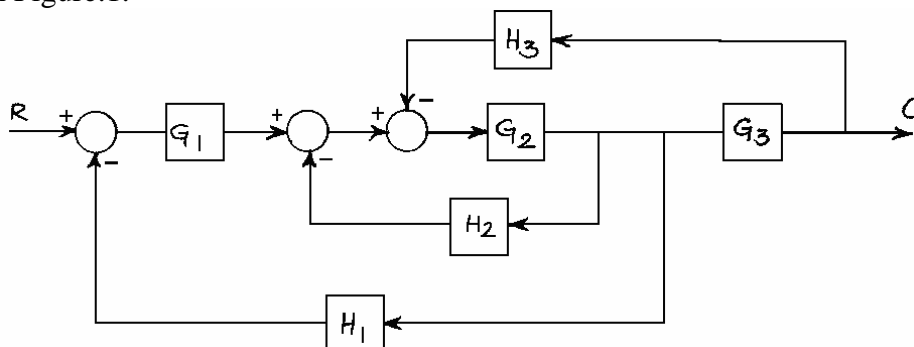


Figure.1

3. To improve the transfer behaviour of the system, having a forward transfer function $G(s) = \frac{25}{s(s+2)}$ a controller with proportional and derivative action is added, as shown in Figure.2 below. Determine the value of K such that the resulting system will have a damping ratio of 0.5. What is the response $C(t)$ of this resulting system to a unit step function excitation $r(t) = u(t)$ when all initial conditions are zero. [15]

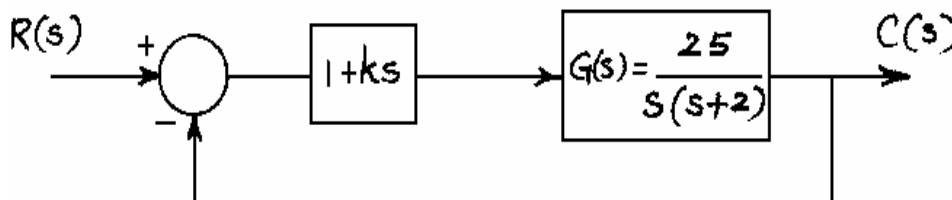


Figure.2

4. Construct the root locus diagram for the system given in Figure.3 below. Hence or otherwise find
- The maximum and minimum values of K for system stability and
 - The value of K in the system characteristic equation that gives a damping ratio of 0.5. [15]

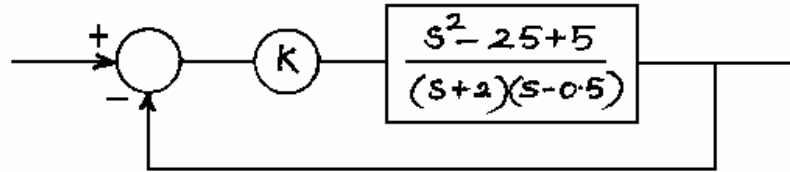


Figure.3

5. Sketch the Bode plot for the following transfer function and determine the system gain K for the gain cross over frequency ω_c to be 5 rad/sec. [15]

$$G(s) = \frac{Ks^2}{(1 + 0.2s)(1 + 0.02s)}$$

- State and explain the Nyquist stability criterion.
- Sketch the Nyquist plot for the transfer function:

$$G(s) H(s) = \frac{52}{(s + 2)(s^2 + 2s + 5)}. \text{ Discuss its stability. [5+10]}$$

- What are different types of compensators available? Explain briefly.
- Show that the lead network and lag network inserted in cascade in an open loop acts as proportional-plus-derivative control (in the region of small ω) and proportional-plus-integral control (in the region of large ω) respectively. [8+7]

- What are the properties of state transition matrix? Explain.
- The state space representation of a system is given by

$$\dot{X} = \begin{bmatrix} -5.0 & 1 \\ -6 & 0.0 \end{bmatrix} X. \text{ Find the value of } x_1(t) \text{ at } t=1, \text{ if } x_1(0)=1.0 \text{ and } x_2(0)=0$$

[5+10]
