

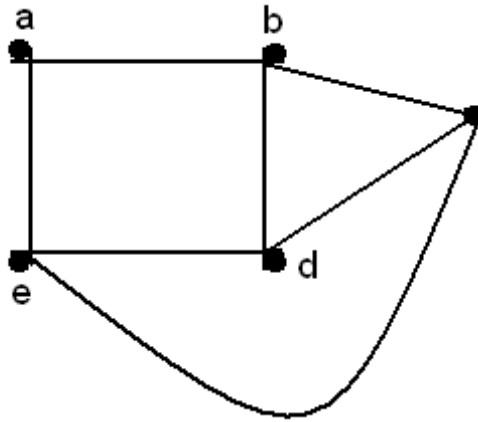
II B.Tech I Semester Examinations, May/June 2012
MATHEMATICAL FOUNDATION OF COMPUTER SCIENCE
Common to Information Technology, Computer Science And Engineering,
Computer Science And Systems Engineering

Time: 3 hours

Max Marks: 80

Answer any FIVE Questions
All Questions carry equal marks

1. (a) Prove the equivalence: $(\sim P \wedge (\sim Q \wedge R)) \vee (Q \wedge R) \vee (P \wedge R) \Leftrightarrow R$
(b) Show that C is a logical consequence of the formula:
 $A \wedge (A \rightarrow (B \vee C)) \wedge (B \rightarrow \sim A)$
using truth tables. [8+8]
2. (a) Explain, in detail, the algebraic systems: Group, Abelian Group and Monoid.
with suitable examples.
(b) Give an example of a monoid which is NOT a group. [8+8]
3. (a) Let the relation $R = \{(a, b) \mid a - b \text{ is divisible by } 3\}$ on the set,
 $S = \{1, 2, 3, 5, 6, 7\}$. Show that R is an equivalence relation and draw the
graph of R .
(b) Using the Pigeonhole Principle, show that: "*there must be at least 90 ways*
to choose numbers from 1 to 15 so that all the choices have the same sum."
[8+8]
4. (a) Write the rules for constructing Hamiltonian paths and cycles.
(b) Write the difference between Hamiltonian graphs and Euler graphs. [8+8]
5. (a) Determine the coefficient of x^5 and x^4 in $(a+bx+cx^2)^{10}$
(b) What is the sum of all numbers of the form $12! / q_1! q_2! q_3!$, where $q_1, q_2,$
 q_3 range over all the sets of nonnegative integers such that $q_1+q_2+q_3=12$?
[8+8]
6. (a) Write the algorithm for breadth first search spanning tree. Explain how the algorithm.
(b) Apply breadth first search on the following figure work with an example. [6+10]



7. Write the quantifiers of the following statements, where predicate symbols denotes, $F(x)$: x is fruit, $V(x)$: x is vegetable and $S(x, y)$: x is sweeter than y .
- Some vegetable is sweeter than all fruits
 - Every fruit is sweeter than all vegetables
 - Every fruit is sweeter than some vegetables
 - Only fruits are sweeter than vegetables. [16]
8. Chose an appropriate substitution to translate $a_n = 2 a_{n/4} + n$ for $n=4^k \geq 4$ and $a_1=1$ in to a first order relation. Solve this relation by underdetermined coefficients and then find a_{4k} . [16]

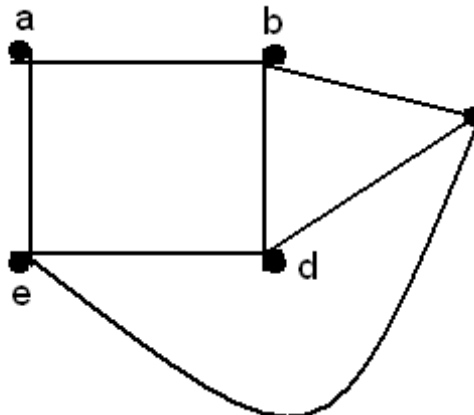
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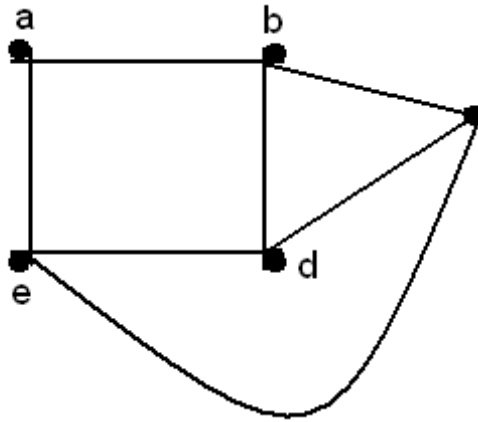
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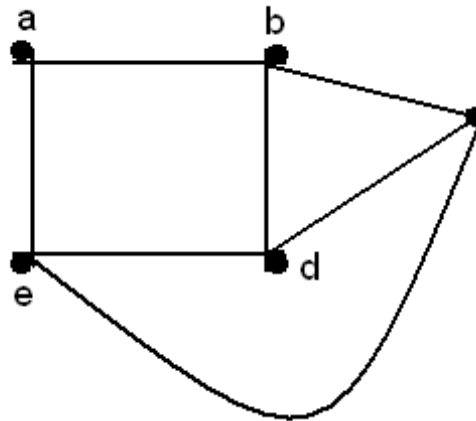
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