

Time: 3 Hours

Max. Marks: 75

Note: This question paper contains two parts A and B.  
Part A is compulsory which carries 25 marks. Answer all questions in Part A.  
Part B consists of 5 Units. Answer any one full question from each unit.  
Each question carries 10 marks and may have a, b, c as sub questions.

## PART-A

(25 Marks)

- 1.a) Draw the sampling function and mention its properties. [2]
- b) What are Dirichlet conditions? [3]
- c) Find the Fourier transform of unit step signal. [2]
- d) Define aliasing. [3]
- e) Distinguish between LTI and LTV systems. [2]
- f) Define Signal Bandwidth and System Bandwidth. [3]
- g) Show that  $x(t) * \delta(t) = x(t)$ . [2]
- h) State and prove Parseval's Theorem. [3]
- i) Find the Laplace Transform of  $x(t) = e^{-at} u(t)$  [2]
- j) Find the z transform of the sequence  $x[n] = \{5, 3, -2, 0, 4, -3\}$  [3]

## PART-B

(50 Marks)

- 2.a) Explain how a function can be approximated by a orthogonal functions.
  - b) Discuss the concept of Impulse function. Explain how signum function is expressed in terms of unit step function? [5+5]
- OR
- 3.a) Consider full rectified sine wave with peak amplitude '1' and time period '1', expand this using exponential Fourier series. Also sketch the spectrum.
  - b) Derive the relation between Trigonometric and exponential Fourier series coefficients. [5+5]
- 4.a) State and prove time convolution and time differentiation properties of Fourier transform.
  - b) Find the Fourier transform of the signal  $x(t) = \frac{1}{a^2 + t^2}$ ? [5+5]
- OR
- 5.a) What is sampling? Explain the need for sampling and clearly discuss the process of sampling low pass signals and derive conditions for optimum reconstruction of signal.
  - b) Distinguish natural and flat top sampling. [5+5]
- 6.a) Explain properties of LTI system.
  - b) Show that from the knowledge of the impulse response  $h(t)$  of a linear system, the response of any arbitrary function can be obtained. [5+5]
- OR
- 7.a) Obtain the conditions for the distortion less transmission through a System.
  - b) Explain causality and physical realizability of a system and hence give poly-wiener criterion. [5+5]

- 8.a) Find the Auto-Correlation of  $f(t) = \cos(\omega_0 t)$  and sketch. [5+5]  
b) Explain about graphical procedure to perform convolution, with an example.

OR

- 9.a) Explain detection of periodic signals in the presence of noise by Correlation.  
b) Derive the relation between PSDs of input and output for an LTI system. [5+5]

10. Find Laplace transforms and sketches their ROC of  $x(t) = e^{-a|t|}$  for  $a > 0$  and  $a < 0$ . Find the inverse Laplace transform of  $X(s) = \frac{5s+13}{s(s^2+4s+13)}$   $\text{Re}(s) > 0$ . [10]

OR

- 11.a) Determine  $z$ -transform and sketch the ROC of the following signal  $x[n] = a^{|n|}$  for  $a < 1$  and  $a > 1$ .  
b) Find the inverse  $z$ -transform of  $X(z) = \frac{z}{z(z-1)(z-2)^2}$  with ROC  $|z| > 2$ . [5+5]

--ooOoo--

OR