**R16** JAWAHARLAL NEHRU TEÇHNOLOGICAL UNIVERSITY HYDERABAD Code No: 133BD B.Tech II Year I Semester Examinations, April/May - 2018 MATHEMATICS - IV (Common to CE, EEE, ME, ECE, CSE, EIE, IT, MCT, MMT, AE, MIE, PTM, CEE, MSNT) Max. Marks: 75 Time: 3 Hours Note: This question paper contains two parts A and B. Part A is compulsory which carries 25 marks. Answer all questions in Part A. Part B consists of 5 Units. Answer any one full question from each unit. Each question carries 10 marks and may have a, b, e as sub questions. PART- A (25 Marks) [2] Show that  $u = \frac{x}{x^2 + y^2}$  is harmonic [3] 1.a) Write Cauchy-Riemann equations in polar form. [2] b) Expand  $f(z) = \sin z$  in Taylor's series about  $z = \frac{\pi}{4}$ [3] c) Find residue of  $f(z) = \frac{z}{z^2+1}$  at its poles Find image of the circle |z| = 2 under the transformation w = z + 3 + 2i[2] Determine the region of w-plane into which the region is mapped by the Find the value  $b_n$  of the Fourier series of the function  $f(x) = x^2 - 2$ , when  $-2 \le x \le 2$ g) Find the Fourier sine transformation of  $2e^{-5x} + 5e^{-2x}$ Classify the equation  $3\frac{\partial^2 u}{\partial x^2} + 6\frac{\partial^2 u}{\partial x^2} + 4\frac{\partial^2 u}{\partial x \partial y} - 2\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} - 4 = 0$ [3] Write the one dimensional Heat equation in steady state. PART-B (50 Marks)







