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CMR ENGINEERING COLLEGE:: HYDERABAD **UGC AUTONOMOUS**

II-B. TECH-I-Semester End Examinations (Supply) - August - 2023 COMPUTER ORIENTED STATISTICAL METHODS

(CSD) [Time: 3 Hours] [Max. Marks: 70] Note: This question paper contains two parts A and B. Part A is compulsory which carries 20 marks. Answer all questions in Part A. Part B consists of 5 Units. Answer any one full question from each unit. Each question carries 10 marks and may have a, b, c as sub questions. **PART-A** (20 Marks) If the probability is 0.05 that a certain kind of measuring device will show excessive drift, what is the [2M]probability that the sixth measuring device tested will be the first to show excessive drift? State Baye's theorem. b) [2M] c) A random variable X has the following probability distribution. [2M] X 0 1 2 3 5 6 8 P(X)3a 5a lla 13a 15a 17a Find the value of a. If the mean of Binomial distribution is 3 and variance is 9/4, obtain the value of n. [2M] If X is normal distributed with mean 2 and variance 0.1, then find P (|X-2|) \geq 0.01? [2M] A sample size 10 was taken from a population S.D. of samples 0.03, find the maximum error with 99% [2M] confidence. Define unbiased estimator. g) [2M] h) Write about type I error and type II error. [2M] Define the Stochastic Process. i) [2M] Write Advantages of Markov Analysis. [2M] **PART-B** (50 Marks) 2.a) If two dice are thrown, what is the probability that the sum is [5M] i. greater than 8 ii. neither 7 nor 11? There are three boxes. [5M] I contains- 14 light bulbs out of which 8 are defective II contains- 10 light bulbs out of which 4 is defective III contains- 12 light bulbs out of which 5 are defective. A box is chosen at random and a bulb is selected. If it is defective, find the probability that it is from i. Box- I ii. Box-II iii. Box-III OR 3.a) Three students A, B, C are running race. A and B have the same probability of winning and each is [5M] twice as likely to win as C. Find the probability that B or C wins. Define discrete probability distribution, continuous probability distribution. Give an example of each. [5M]

- 4.a) The probability density f(x) of a continuous random variable is given by $f(x) = c e^{-|x|}$, $-\infty < x < \infty$. [5M] Show that $c = \frac{1}{2}$ and find the mean of the distribution.
- b) Ten coins are thrown simultaneously. Find the probability of getting at least
 i. Seven heads
 ii. Six heads
 iii. one head

OR

- 5.a) A sample of 4 items is selected at random from a box containing 12 items of which 5 are defective. [5M] Find the expected number E of defective items.
 - b) A coin is biased in a way that a head is twice as likely to occur as a tail. If the coin is tossed 3 times, find the probability of getting 2 tail and one head.
- 6. In normal distribution, 7% of the items are under 35 and 89% are under 63. Determine the mean and [10M] variance of the distribution.

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- 7.a) The claim that the variance of a normal population is $\sigma^2 = 21.3$ is rejected if the variance of random sample of size 15 exceeds 39.74. What is the probability that the claim will be rejected even though $\sigma^2 = 21.3$?
 - b) A random sample of size 100 is taken from an infinity population having the mean $\mu = 76$ and variance $\sigma^2 = 256$. What is the probability that \bar{x} (sample mean) will be between 75 and 78.
- 8.a) Among the items produced by a factory out of 800, 65 were defective. In another sample out of 300, 40 were defective. Test the significance between the difference of two proportion at 1% level.
 - b) From the following data, find whether there is any significance likely in the habit of taking soft drinks among the categories of employees. Use Chi-Square distribution test with level of significance 0.05

Employees						
Soft drinks	Clerks	Teachers	Officers			
Pepsi	10	25	65			
Thumsup	15	30	65			
Fanta	50	60	30			

OR

- 9.a) An ambulance service claims that it takes on the average less than 10 minutes to reach its destination in emergency calls. A sample of 36 calls has a mean of 11 minutes and variance of 16 minutes. Test the claim at 0.05 level of significance.
 - The blood pressures of 5 women before and after intake of a certain drug are given below. Test whether there is significant change in blood pressure at 1% level of significance.

Before	110	120	125	132	125
After	120	118	125	136	121

- 10. Suppose an urn A contains 2 white marbles and urn B contains 4 red marbles. At each step of the process, [10M] a marble is selected at random from each urn and the two marbles selected are interchanged. Let Xn denote the number of red marbles in urn A after n interchanges.
 - i. Find the transition matrix P.
 - ii. What is the probability that there are 2 red marbles in urn A after 3 steps.

11. The transition probability matrix of Markov chain $\{X_n\}$;

[10M]

[5M]

$$n = 1,2,3....$$
 having 3 states 1,2 and 3 is $P = \begin{bmatrix} 0.1 & 0.5 & 0.4 \\ 0.6 & 0.2 & 0.2 \\ 0.3 & 0.4 & 0.3 \end{bmatrix}$. Is the matrix irreducible.