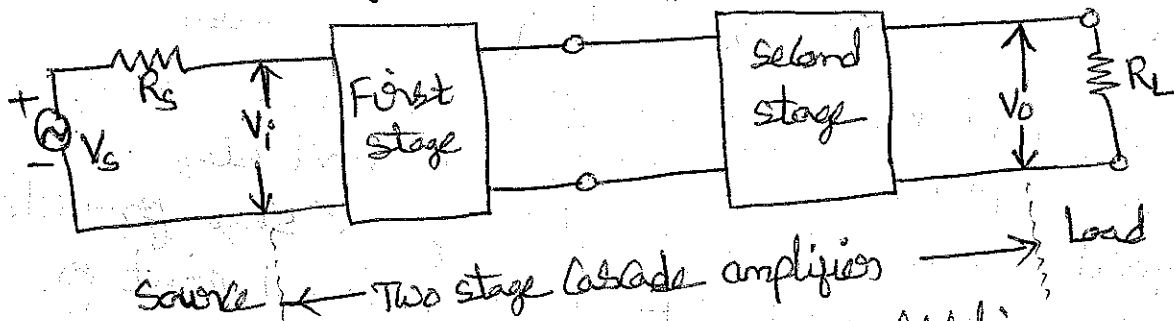


Need for Cascading:

- If the voltage or power gain obtained from a single stage small signal amplifier is not sufficient for a practical application, one has to use more than one stage of amplification to achieve necessary voltage and power gain. Such an amplifier is called a multistage amplifier.
- In multistage amplifier, the output of one stage is fed as the input to the next as shown in figure:



- Such a connection is commonly preferred to as cascading.
- In amplifiers, cascading is also done to achieve correct input and output impedances for specific applications.
- Depending upon the type of amplifiers used in individual stages, multistage amplifiers can be classified into several types.
- A multistage amplifier using two or more single stage CE amplifiers is called as cascaded amplifiers.
- A multistage amplifier with CE as the first stage and CB as the second stage is called as cascode amplifier. Such cascode and cascade connections are also possible in FET amplifiers.

Different coupling schemes used in amplifiers:

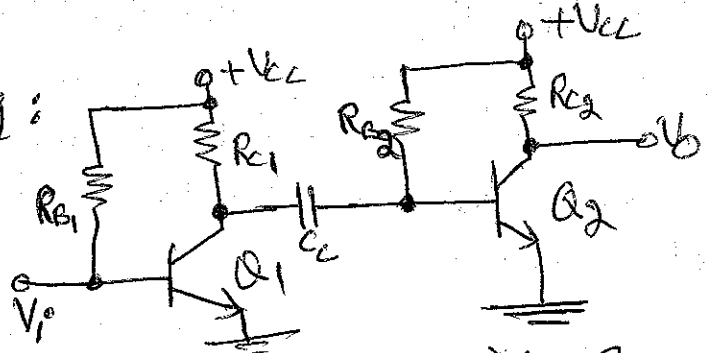
- when amplifiers are cascaded, it is necessary to use a coupling network between the output of one amplifier and the input of the following amplifier. This type of coupling is called interstage coupling.
- These coupling networks serve the following two purposes:
  - 1) It transfers the ac output of one stage to the input of the next stage.
  - 2) It isolates the dc conditions of one stage to the next.

→ The Coupling schemes commonly used in multistage amplifiers are,

- ① RC Coupling
- ② Transformer Coupling
- ③ Direct Coupling

### Resistance Capacitance (RC) Coupling:

→ It is the most commonly used discrete device amplifiers as it is least expensive and has satisfactory frequency response.



→ In this method the signal developed across the collector resistor  $R_C$  of each stage is coupled through capacitor  $C_C$  into the base of the next stage.

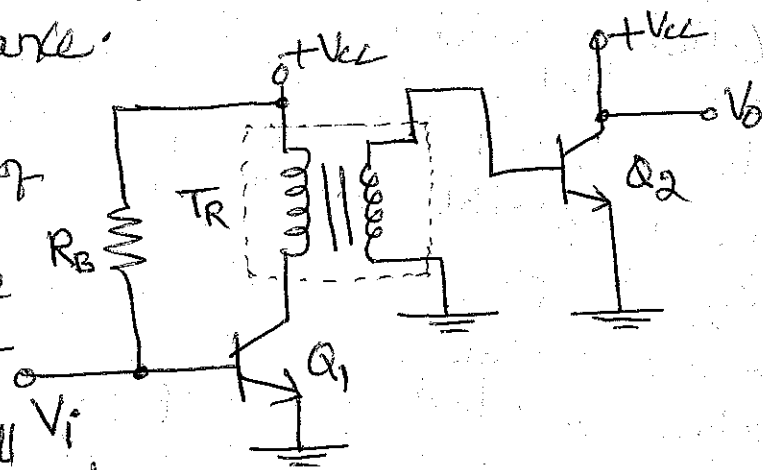
→ The coupling capacitor  $C_C$  isolates dc conditions of one stage from the following stage, hence it does not affect the quiescent point of the following stage.

→ The RC network is broadband in nature. Therefore it gives a wideband frequency response without peak at any frequency and here used to cover a complete AF amplifier bands.

→ However its frequency response drops off at very low frequencies due to coupling capacitors and also at high frequencies due to shunt capacitors such as stray capacitance.

### Transformer Coupling:

→ In this method, the primary winding of the transformer acts as a collector load and the secondary winding transfers the ac output signal directly to the base of the next stage.



→ Such a coupling increases the overall circuit gain and the level of interstage impedance matching.

→ However transformers with broad frequency response are very expensive and hence, this type of coupling is restricted mostly to power amplifiers where efficient impedance matching is a critical requirement for maximum power transfer and efficiency.

→ Frequency response of transformer coupled amplifier is poor in comparison with that of an RC coupled amplifier. Its leakage inductance and interwinding capacitance does not allow amplifier to amplify the signals of different frequencies equally well.

→ Interwinding capacitance of the transformer coupled may give rise resonance at certain frequency which makes amplifier to give very high gain at that frequency.

→ By putting shunting capacitors across each winding of the transformer we can get resonance at any desired RF frequency. Such amplifiers are called tuned voltage amplifiers.

→ These provide high gain at the desired frequency i.e. they amplify selectively frequencies. For this reason, the transformer-coupled amplifiers are used in radio and TV receivers for amplifying RF signals.

→ As dc resistance of the transformer winding is very low, almost all dc voltage applied by  $V_{CC}$  is available at the collector. Due to the absence of collector resistance it also eliminates unnecessary power loss in the resistor.

### Direct Coupling:

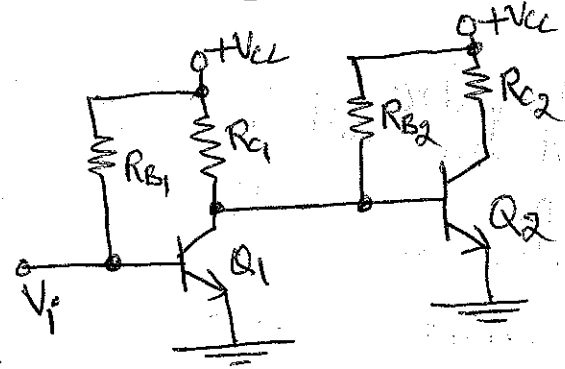
→ In this method the ac output signal is fed directly to the next stage as shown in figure.

→ No reactance is included in the coupling network. Special dc voltage level circuits are used to match the output dc levels.

→ It is used when amplification of low frequency signals is to be done. Further coupling devices such as capacitors, transformers cannot be used at low frequencies because their size becomes very large.

→ This direct coupling allows the quiescent dc collector current of first stage to pass through base of the next stage, affecting its biasing conditions.

→ Due to absence of RC components its low frequency response is good but at higher frequencies shunting capacitors such as stray capacitance reduce the gain of the amplifiers.



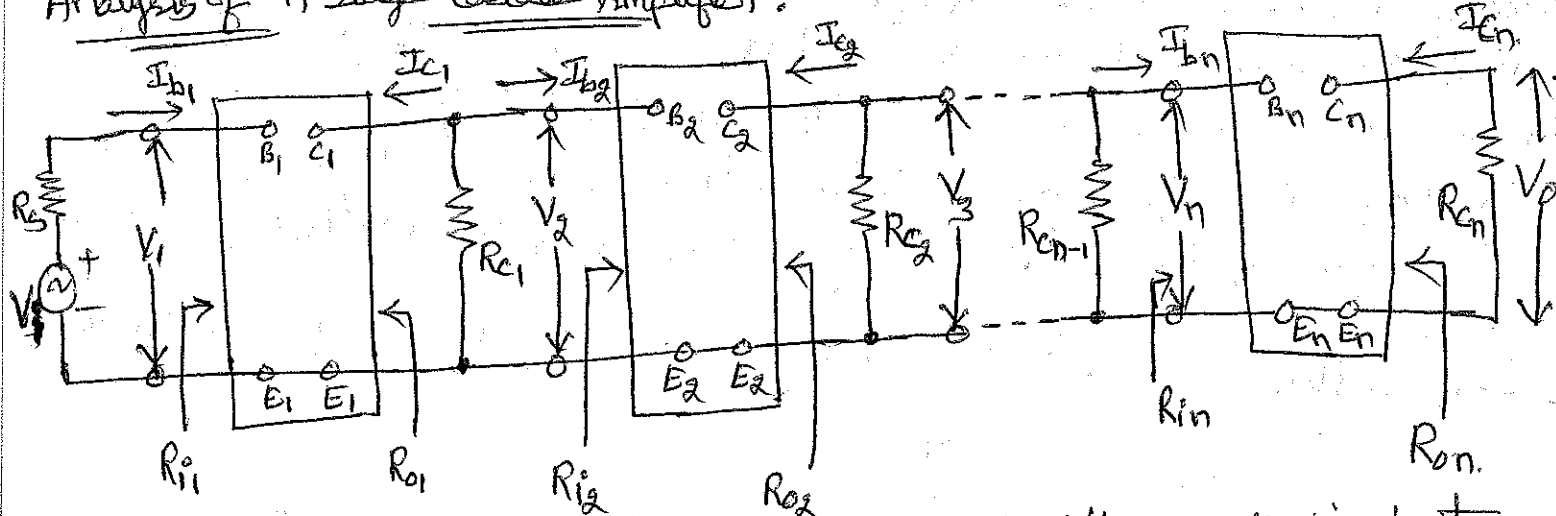
→ The transistor parameters such as  $V_{BE}$  and  $\beta$  change with temperature causing the collector current and voltage to change. Because of direct coupling these changes appear at the base of the next stage and hence in the output.

→ Such an unwanted change in the output is called drift and it is a serious problem in the direct coupled amplifiers.

Comparison between various coupling methods:

Parameter	RC Coupled	Transformer Coupled	Direct Coupled.
1) Coupling Components	Resistor & Capacitor	Impedance matching transformer	— No
2) Block DC	Yes	Yes	— No
3) Frequency response	Flat at middle frequencies	Not uniform, high at resonant frequency and low at other frequencies	Flat at middle frequencies and improvement in the low frequency response.
4) Impedance matching	Not achieved	Achieved	Not achieved Yes
5) DC amplification	No	No	—
6) Weight	Light	Bulky & heavy	— present
7) Drift	Not present	Not present	— Not present
8) Hum	Not present	present	— Not present
9) Application	used in all audio small signal amplifiers, used in record players, tape recorders, public address systems, radio receivers and television receivers	used in amplifiers where impedance matching is an important criteria. used in output stage of the public address system to match the impedance of the loudspeaker. used in the RF amplifier stage of the receiver as a tuned voltage amplifier	used in amplification of slow varying parameters and where DC amplification is required

Analysis of 'n' stage Cascade Amplifier:



Voltage gain: In a multistage amplifier, the output voltage of the first stage acts as the input voltage of second stage and so on. The voltage gain of the complete cascade amplifier is equal to the product of the voltage gains of the individual stages.

Proof: The voltage gain of the first stage,

$$A_{v1} = \frac{V_2}{V_1} = \frac{\text{output voltage of first stage}}{\text{input voltage of first stage}} = A_{v1} \angle \theta_1$$

where  $A_{v1}$  is the magnitude of voltage gain and  $\theta_1$  is phase angle of the output voltage relative to input voltage.

$$\text{Similarly } A_{v2} = \frac{V_3}{V_2} = \frac{\text{output voltage of second stage}}{\text{input voltage of second stage}} = A_{v2} \angle \theta_2$$

The resultant voltage gain,  $A_v = \frac{V_o}{V_1} = \frac{\text{output voltage of } n^{\text{th}} \text{ stage}}{\text{input voltage of first stage}}$

$$A_v = A_v \angle \theta$$

But,

$$\frac{V_o}{V_1} = \frac{V_2}{V_1} \cdot \frac{V_3}{V_2} \cdot \frac{V_4}{V_3} \cdot \dots \cdot \frac{V_n}{V_{n-1}} \cdot \frac{V_o}{V_n}$$

$$A_v = A_{v1} \cdot A_{v2} \cdot A_{v3} \cdot \dots \cdot A_{vn} \cdot \angle \theta_1 + \angle \theta_2 + \angle \theta_3 + \dots + \angle \theta_n$$

$$= A_v \angle \theta$$

Hence

$$A_v = A_{v1} \cdot A_{v2} \cdot A_{v3} \cdot \dots \cdot A_{vn}$$

$$\theta = \theta_1 + \theta_2 + \theta_3 + \dots + \theta_n$$

Hence for multistage cascode amplifier,

(i) the magnitude of the resultant voltage gain equals the product of the magnitudes of the voltage gains of the individual stages.

(ii) the phase shift of the resultant voltage gain equals the sum of the phase shifts of the individual stages comprising the multistage cascode amplifier.

→ The voltage of the  $K^{\text{th}}$  stage of the  $n$  stage cascode amplifier is given by,

$$A_{VK} = \frac{A_{IK} \cdot R_{LK}}{R_{IK}}$$

where  $R_{LK}$  is the effective load impedance at the collector of the  $K^{\text{th}}$  stage and  $R_{IK}$  is the input impedance of the  $K^{\text{th}}$  stage.

→ The terms  $A_{IK}$ ,  $R_{LK}$  and  $R_{IK}$  may be evaluated by starting from the last stage and proceeding backward to the first stage.

$$\text{Current gain } A_{In} = \frac{-h_{fe}}{1 + h_{oe} R_{Ln}}$$

$$\text{Input Resistance } R_{In} = h_{ie} + h_{oe} A_{In} \cdot R_{Ln}$$

where  $R_{Ln}$  is the effective load impedance for the last stage and equals  $R_{en}$ .

→ The effective load impedance  $R_{e(n-1)}$  of the  $(n-1)^{\text{th}}$  stage is equal to,

$$R_{e(n-1)} = R_{e(n-1)} \parallel R_{i(n)} = \frac{R_{e(n-1)} \cdot R_{i(n)}}{R_{e(n-1)} + R_{i(n)}}$$

Having known  $R_{e(n-1)}$ ,  $A_{I(n-1)}$  can be found out from,

$$A_{I(n-1)} = \frac{-h_{fe}}{1 + h_{oe} R_{e(n-1)}}$$

$$\text{and } R_{i(n-1)} = h_{ie} + h_{oe} A_{I(n-1)} \cdot R_{e(n-1)}$$

→ By proceeding in this manner one can calculate the current gain and input impedance of each stage including the first.

Current gain: In order to find the resultant voltage gain, the voltage gain of the individual stages can be found out and the product of these gains give the resultant voltage gain.

→ Alternatively the resultant voltage gain can be found directly by the relation,

$$A_V = \frac{A_I R_{in}}{R_{in}}$$
 where  $A_I$  is the current gain of the complete n-stage amplifier.

But 
$$A_I = \frac{I_o}{I_{b1}} = \frac{-I_{cn}}{I_{b1}} = \frac{-I_{c1}}{I_{b1}} \cdot \frac{I_{c2}}{I_{c1}} \dots \frac{I_{cn}}{I_{c(n-1)}}$$

$$A_I = A_{I1} \cdot A'_{I2} \cdot A'_{I3} \dots A'_{In}$$

Here  $A_{I1}$  is the base to collector gain of the first stage and equals  $\frac{I_{c1}}{I_{b1}}$ , while  $A'_{I2}, A'_{I3}$  are the collector to collector current gains of second and third stages.

For the k<sup>th</sup> stage the collector to collector current gain is given by,

$$A'_{Ik} = \frac{I_{ck}}{I_{c(k-1)}}$$

For the same k<sup>th</sup> stage, the base to collector current gain is given by,

$$A_{Ik} = \frac{-I_{ck}}{I_{bk}}$$

These two current gains can be related by the equation,

$$A_{Ik} = A'_{Ik} \cdot \frac{R_{c(k-1)}}{R_{c(k-1)} + R_{ik}}$$

The procedure for calculating the resultant current gain  $A_I$  is as follows

① Find the base to collector current gain  $A_{In}$  for the last stage i.e n<sup>th</sup> stage

$$A_{In} = \frac{-h_{fe}}{1 + h_{oe} R_{in}}$$

② Find input impedance of n<sup>th</sup> stage,

$$R_{in} = h_{ie} + h_{oe} A_{In} \cdot R_{cn}$$

$h_{oe} R_{in} = \dots$   
 $h_{oe} R_{in} = \dots$

③ Calculate the effective load resistance  $R_{L(n-1)}$  for the last stage,

$$R_{L(n-1)} = R_{C(n-1)} \parallel R_{in}$$

④ Calculate,

$$A_{I(n-1)} = \frac{-h_{fe}}{1 + h_{oe} R_{L(n-1)}}$$

Proceed in this manner to find  $A_{IK}$ .

⑤ Find the collector to collector current gain  $A'_{IK}$  for the  $K^{th}$  stage using

$$A'_{IK} = A_{IK} \cdot \frac{R_{C(K-1)}}{R_{C(K-1)} + R_{IK}}$$

⑥ Find the resultant current gain  $A_I$  of the  $n$ -stage cascaded amplifier using

$$A_I = A_{I1} \cdot A'_{I2} \cdot A'_{I3} \cdot \dots \cdot A'_{In}$$

Power gain: The power gain of  $n$ -stage amplifier is given by,

$$A_p = \frac{\text{output power of last stage}}{\text{Input power of first stage}}$$

$$A_p = \frac{V_o \cdot I_o}{V_i \cdot I_{b1}} = \frac{-V_o I_{cn}}{V_i \cdot I_{b1}}$$

$$A_p = A_v \cdot A_I$$

Substituting,  $A_v = A_I \cdot \frac{R_{cn}}{R_{id}}$

$$A_p = A_I^2 \cdot \frac{R_{cn}}{R_{id}}$$

Input Impedance: By starting from ~~last~~ stage and proceeding towards the first, the input impedance can be found out as follows,

①  $A_{in} = \frac{-h_{fe}}{1 + h_{oe} R_{cn}}$

②  $R_{in} = h_{ie} + h_{re} \cdot A_{in} \cdot R_{cn}$

③  $R_{L(n-1)} = R_{C(n-1)} \parallel R_{in}$



④ Calculate  $A_{v(n-1)}$ ,  $R_{i(n-1)}$  and  $R_{o(n-2)}$  from above equations.

⑤ proceed in this manner to find the effective input impedance  $R_i$  of the first stage.

output Impedance: The output Impedance of each transistor amplifier stage and that of the complete multistage amplifiers may be calculated starting from the first stage.

The output admittance of first transistor is,

$$Y_{o1} = h_{oe} - \frac{h_{fe} h_{me}}{h_{ie} + R_s}$$

$R_{o1} = \frac{1}{Y_{o1}}$  gives the output impedance of the first transistor.

Parallel combination of  $R_{o1}$  with  $R_{i1}$  forms the output impedance of the first stage.

$$R_{ot1} = \frac{R_{o1} \cdot R_{i1}}{R_{o1} + R_{i1}}$$

This  $R_{ot1}$  forms the source impedance of the second stage.

Again using above equations find  $Y_{o2}$  with  $R_s$  replaced by  $R_{ot1}$

Kind  $R_{ot2} = R_{o2} \parallel R_{i2}$  where  $R_{o2} = \frac{1}{Y_{o2}}$

||ly proceed to find output impedance of the last stage.

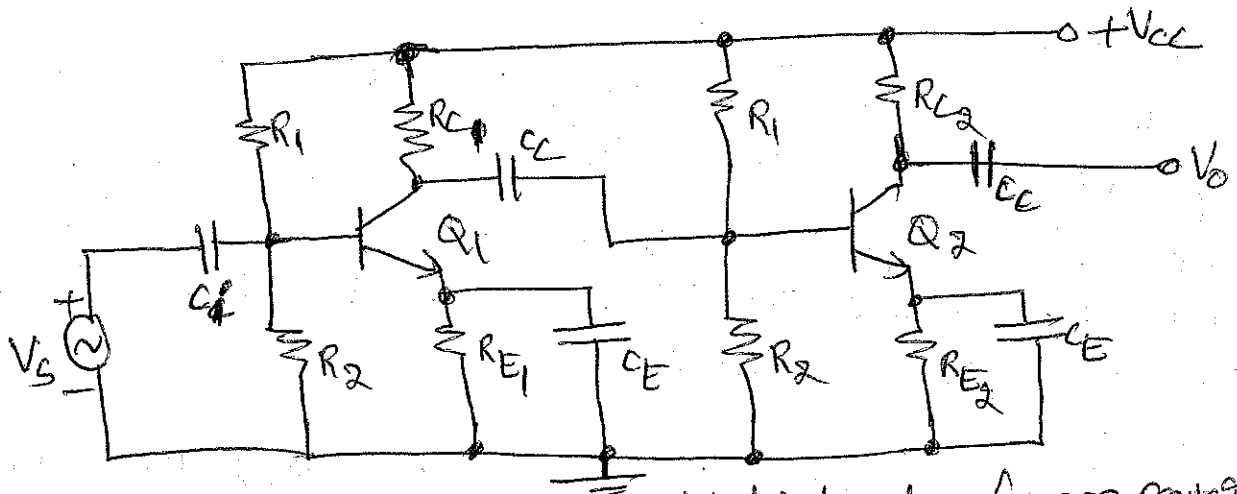
Notes: The above methods can be used for CB and CC configurations also as well as for combination of these three configurations.

## Selection of Configuration in Cascading Amplifiers:

Characteristics	CB	CE	CC
1) $R_i$	Very low	Low	High
2) $R_o$	Very high	High	Low
3) $A_v$	Medium	Medium	Low
4) $A_i$	Less than unity	High	High

- From design point of view multistage amplifier is divided into three parts, Input stage, middle stages and output stage.
- Input stage is designed such that its input impedance matches with the source impedance and the output stage is designed such that its output impedance matches with the load impedance. The remaining middle stages are designed to provide necessary power (Voltage as well as Current) gain.
- CB Configuration is selected for input stage because the input impedance of the CB Configuration matches with a very low source impedance.
- CE Configuration provides Voltage as well as Current gain here it is the best choice for the middle stages.
- CC Configuration is selected for output stage because the output impedance of CC Configuration is low and matches with load impedance.

Two stage RC Coupled Amplifier :



- The two transistors  $Q_1$  and  $Q_2$  are identical and a common power supply is used.
- $R_C$  is the collector (load) resistor, resistors  $R_1$ ,  $R_2$  and  $R_E$  provide the required bias.
- The bypass capacitor  $C_E$  prevents loss of amplification due to negative feedback.
- The output of the first stage gets coupled to the input of the second stage via coupling capacitor  $C_C$  which also serves as the blocking capacitor to keep the DC component of the output of the first stage from reaching the input of the second stage and to pass AC component.

operation :

- The AC input signal applied at the base is amplified by the transistor  $Q_1$ . Its phase is reversed and the amplified output appears across its collector load  $R_C$ .
- The output of the first stage across  $R_C$  is given to the base of second stage transistor  $Q_2$  through the coupling capacitor  $C_C$ .
- This signal at the base of  $Q_2$  is further amplified and its phase is again reversed. Hence the output signal is the twice amplified replica of the input signal. The output signal is in phase with the input signal because it has been reversed twice.
- In the mid frequency range, the gain is constant because the coupling and bypass capacitors are as good as short circuits, on both sides of the mid frequency range, the gain decreases.
- At high frequencies, the value  $\beta$  of the transistor decreases. Hence the reactance of the capacitor  $C_C$  increases with the reduction in frequency of the signal, the voltage gain of the amplifier reduces.

→ At very low and very high frequencies, the gain of the amplifier reduces to almost zero.

### Advantages of RC Coupling:

- 1) It requires cheap components like resistors and capacitors and not expensive or bulky components. Hence it is small, light and inexpensive.
- 2) It gives uniform voltage amplification over a wide frequency range from a few Hz to a few MHz because resistor values are independent of frequency changes. Hence RC coupled amplifier can be used to great advantage in speech, music etc.
- 3) Since it does not use any coil or transformer which may pick up unwanted signals, it has minimum possible non-linear distortion. Hence there is no magnetic field to ~~interfere~~ interface with the signal.
- 4) Its overall amplification is higher than that of the other couplings.

### Disadvantages of RC Coupling:

- 1) Due to large drop across collector load resistors, the collector circuit at relatively small voltages unless higher supply voltage is used to overcome this voltage drop.
- 2) It is noisy in humid weather.
- 3) The impedance matching is poor as the output impedance of the RC coupled amplifier is several hundred ohms while that of a speaker is only a few ohms. Hence, the amount of power transferred to the speaker is reduced.

### Differences in performance of an RC Coupled Amplifier over Single Stage:

- 1) Its overall amplification is higher.
- 2) Its non-linear distortion is less.
- 3) It has better fidelity over a wide frequency range.
- 4) Its frequency response is much better over the audio frequency range.

Applications:

→ Since audio fidelity is excellent over a wide range of frequencies, the RC coupled amplifier is extensively employed as a voltage amplifier eg. in the initial stages of a public address system. However, as the impedance matching is poor, reduced power is transferred to the speaker.

A.C Analysis:

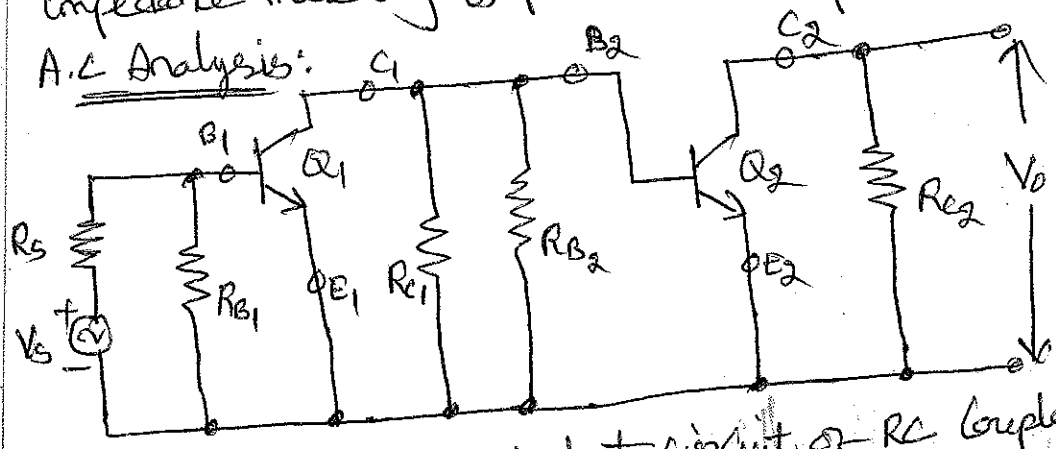


Fig (b) AC equivalent circuit of RC Coupled Amplifier

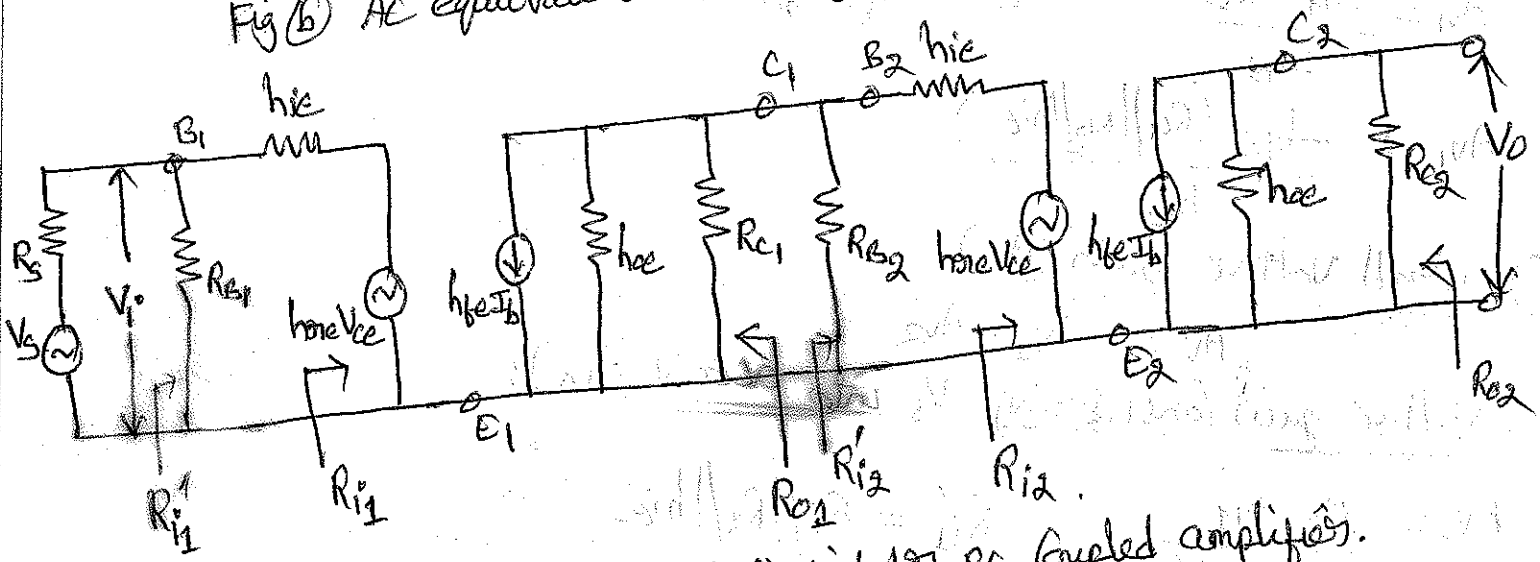


Fig (c) h-parameter equivalent circuit for RC Coupled amplifier.

Second stage analysis:

Current gain (Aiz):

$$A_{i2} = \frac{-h_{fe}}{1 + h_{oe} R_L} = \frac{-h_{fe}}{1 + h_{oe} R_{eq}}$$

{  $\because R_L = R_{eq}$  }

$A_{i2} = -h_{fe}$

{  $\because$  neglecting  $h_{oe} R_{eq}$  }

Input impedance (Zi2):

$Z_{i2} = h_{ie} // R_{B2}$

where  $R_{B2} = R_1 // R_2$

$Z_{i2} = h_{ie}$

since  $R_{B2} \gg h_{ie}$  hence neglecting  $R_{B2}$ .

③ Voltage gain ( $A_{v2}$ ):

$$A_{v2} = \frac{A_{i2} R_L}{Z_{i2}} = \frac{A_{i2} R_{e2}}{Z_{i2}} = \frac{-h_{fe} R_{e2}}{h_{ie}}$$

First stage analysis:

④ Current gain ( $A_{i1}$ ):

$$A_{i1} = -h_{fe}$$

⑤ Input Resistance ( $R_{i1}$ ):

$$R_{i1} = Z_{i1} = h_{ie}$$

⑥ Voltage gain ( $A_{v1}$ ):

$$A_{v1} = \frac{A_{i1} \cdot R_L}{Z_{i1}} \quad R_L = R_{c1} \parallel R_{e2} \parallel h_{ie}$$

$$A_{v1} = \frac{-h_{fe} (R_{c1} \parallel R_{e2} \parallel h_{ie})}{h_{ie}}$$

⑦ overall voltage gain ( $A_v$ ):

$$A_v = A_{v1} \cdot A_{v2}$$

⑧ Voltage gain considering  $V_s$  into account ( $A_{vs}$ ):

$$A_{vs} = \frac{A_v \cdot R_{i1}'}{R_s + R_{i1}'} \quad R_{i1}' = R_{i1} \parallel R_{e2} \parallel h_{ie}$$

$$A_{vs} = \frac{A_v \cdot (R_{i1} \parallel R_{e2} \parallel h_{ie})}{R_s + (R_{i1} \parallel R_{e2} \parallel h_{ie})}$$

⑨ output Impedance ( $Z_o$ ):

$$Z_{o1} = R_{c1} \parallel h_{oe1}$$

$$Z_{o2} = R_{e2} \parallel h_{oe2}$$

Prob 0: For a CE-CE cascade amplifier find  $R_i$ ,  $A_i$ ,  $A_v$ ,  $R_o$ ,  $R_i'$ ,  $R_o'$  and  $A_{vs}$  if circuit parameters are,  $R_s = 1k$ ,  $R_{e1} = 15k$ ,  $R_{e2} = 100\Omega$ ,  $R_{c2} = 4k$ ,  $R_{e2} = 330\Omega$  with  $R_1 = 200k$  &  $R_2 = 20k$  for first stage and  $R_1 = 47k$  &  $R_2 = 4.7k$  for second stage. Assume that  $h_{ie} = 1.2k\Omega$ ,  $h_{fe} = 50$ ,  $h_{re} = 2.5 \times 10^{-4}$  and  $h_{oe} = 25 \mu A/V$ .

Soln:

Second stage analysis:  $h_{oe} \cdot R_L = h_{oe} \cdot R_{c2} = 25 \times 10^{-6} \times 4 \times 10^3 = 0.1$  we can use approximate analysis.

$$A_{i2} = -h_{fe} = -50$$

$$R_{i2} = h_{ie} = 1.2k\Omega$$

$$A_{v2} = \frac{A_{i2} R_L}{R_{i2}} = \frac{A_{i2} \cdot R_{c2}}{R_{i2}} = \frac{-50 \times 4 \times 10^3}{1.2 \times 10^3} = -166.67$$

Analysis of first stage:  $h_{oe} \cdot R_L = h_{oe} \cdot (R_{c1} \parallel R_1 \parallel R_2 \parallel R_{i2})$

$$h_{oe} \cdot R_L' = 25 \times 10^{-6} (821.8) = 0.022 < 0.1$$

So we can use approximate analysis.

$$A_{i1} = -h_{fe} = -50$$

$$R_{i1} = h_{ie} = 1.2k\Omega$$

$$A_{v1} = \frac{A_{i1} \cdot R_L'}{R_{i1}} = \frac{-50 \times 821.8}{1.2 \times 10^3} = -36.74$$

$$\therefore \text{overall gain } A_v = A_{v1} \cdot A_{v2} = (-166.67) \times (-36.74) = 6123.45$$

$$\text{overall voltage gain } A_{vs} = \frac{A_v \cdot R_i'}{R_s + R_i'}$$

$$R_i' = R_1 \parallel R_2 \parallel R_{i1} = 200k \parallel 20k \parallel 1.2k = 1.13k\Omega$$

$$\therefore A_{vs} = \frac{6123.45 \times 1.13 \times 10^3}{1 \times 10^3 + 1.13 \times 10^3} = 3248.6$$

$$\underline{R_o}: \quad R_{o1} = R_{o1} \parallel R_{e1} = \infty \parallel 15k = 15k$$

$$R_{o2} = R_{o2} \parallel R_{e2} = \infty \parallel 4k = 4k$$

## Cascode Amplifier:

- Cascode amplifier is a composite amplifier pair with a large bandwidth used for RF applications and as a video amplifier.
- It consists of a CE stage followed by a CB stage directly coupled to each other and combines some of the features of both the amplifiers.
- For high frequency applications, CB configuration has the most desirable characteristics. However it suffers from low input impedance ( $Z_i \approx h_{ie}$ ).
- The Cascode configuration is designed to have the input impedance essentially that of CE amplifiers, the current gain that of CE amplifiers, the voltage gain that of CB amplifiers and good isolation between input and output.

### CE-CB Cascode Amplifier:

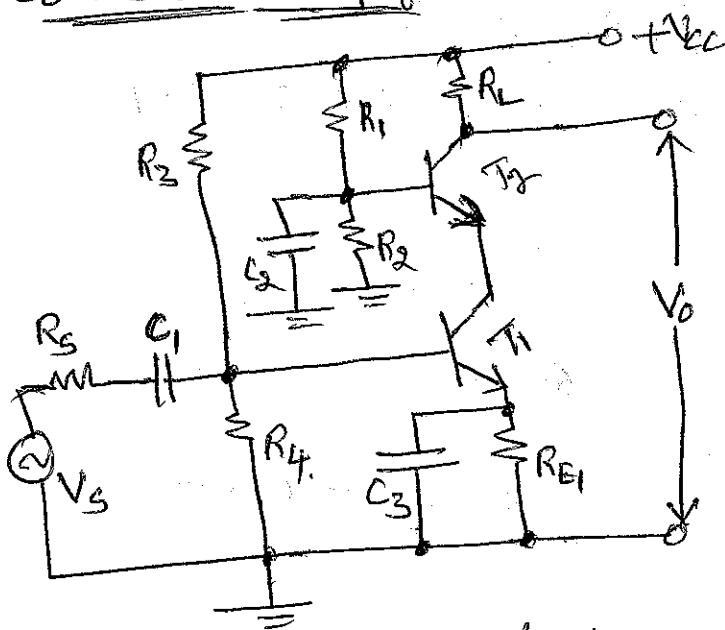


Fig (a) Cascode CE-CB amplifier

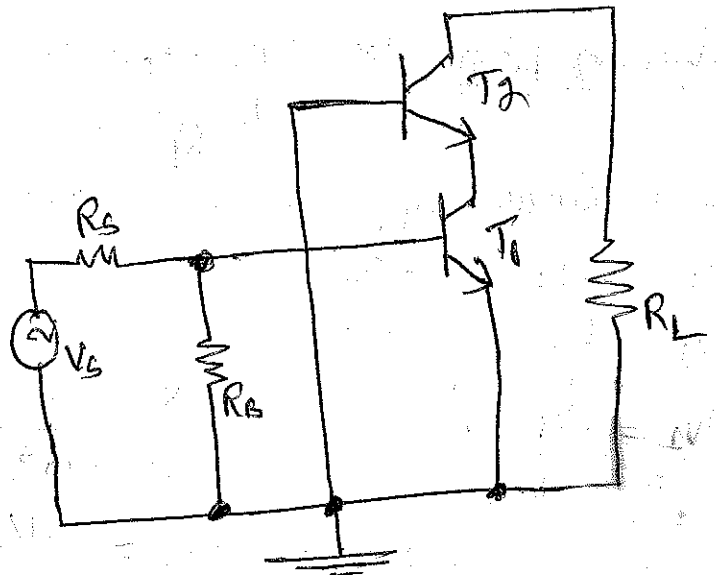
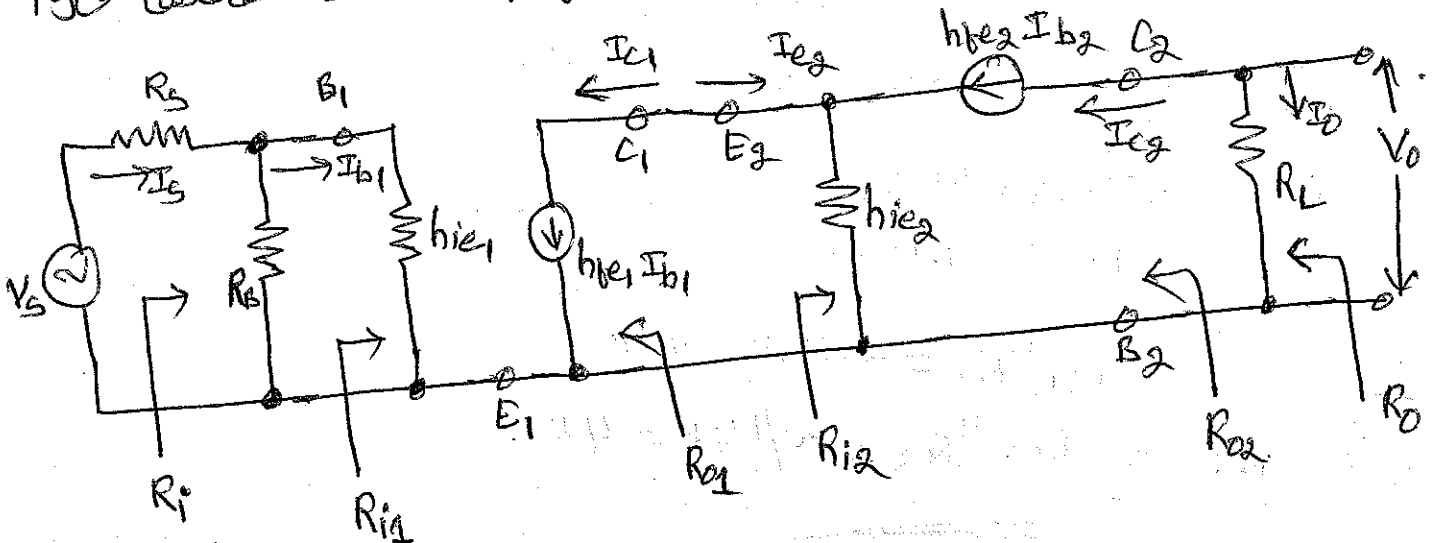


Fig (b) AC equivalent circuit





Let  $R_5 = 1K$ ,  $R_3 = 200K$ ,  $R_4 = 10K$ ,  $R_L = 3K$  and  $h_{ie} = 1.1K$ ,  $h_{fe} = 50$ .

Find  $A_i$ ,  $R_i$ ,  $A_v$ ,  $A_{is}$ ,  $A_{vs}$ ,  $R_o$ .

Second stage (CS amplifier) analysis:

① Current gain  $A_{i2} = \frac{h_{fe}}{1+h_{fe}} = \frac{50}{1+50} = 0.98$

② Input resistance  $R_{i2} = \frac{h_{ie}}{1+h_{fe}} = \frac{1.1 \times 10^3}{1+50} = 21.56 \Omega$

③ Voltage gain  $A_{v2} = \frac{A_{i2} \cdot R_{L2}}{R_{i2}} = \frac{0.98 \times 3 \times 10^3}{21.56} = 136.36$

(or)  $A_{v2} = \frac{h_{fe} R_{L2}}{h_{ie}} = \frac{50 \times 3 \times 10^3}{1.1 \times 10^3} = 136.36$

First stage analysis (CE amplifier)

④ Current gain  $A_{i1} = -h_{fe} = -50$

⑤ Input resistance  $R_{i1} = h_{ie} = 1.1K \Omega$

⑥ Voltage gain  $A_{v1} = \frac{A_{i1} \cdot R_{L1}}{R_{i1}}$  where  $R_{L1} = R_{i2} = 21.56 \Omega$

$$A_{v1} = \frac{-50 \times 21.56}{1.1 \times 10^3} = -0.98$$

⑦ overall voltage gain  $A_v = A_{v1} \cdot A_{v2} = -0.98 \times 136.36 = -133.63$

⑧ overall input resistance  $R_i = R_{i2} \parallel R_5 = R_{i1} \parallel R_3 \parallel R_4 = 1.1K \parallel 200K \parallel 10K = 986.1 \Omega$

⑨ Voltage gain taking  $R_s$  into account,

$$A_{vs} = \frac{V_o}{V_s} = \frac{V_o}{V_i} \cdot \frac{V_i}{V_s} = A_v \cdot \frac{R_i}{R_i + R_s} = -133.63 \times \frac{986.1}{986.1 + 1000} = -66.3$$

⑩ Current gain  $A_{is} = \frac{I_o}{I_s} = \frac{I_o}{I_{e2}} \cdot \frac{I_{e2}}{I_{e2}} \cdot \frac{I_{e2}}{I_{c1}} \cdot \frac{I_{c1}}{I_{b1}} \cdot \frac{I_{b1}}{I_s}$

$I_o = -I_{e2} \Rightarrow \frac{I_o}{I_{e2}} = -1$        $\frac{I_{e2}}{I_{e2}} = 1$        $I_{e2} = -I_{c1} \Rightarrow \frac{I_{e2}}{I_{c1}} = -1$

$\frac{I_{c1}}{I_{b1}} = -A_{i1}$ ,       $\frac{I_{b1}}{I_s} = \frac{R_5}{R_5 + R_{i1}} = \frac{(200K \parallel 10K)}{(200K \parallel 10K) + 1.1K} = \frac{9.524K}{9.524K + 1.1K} = 0.896$

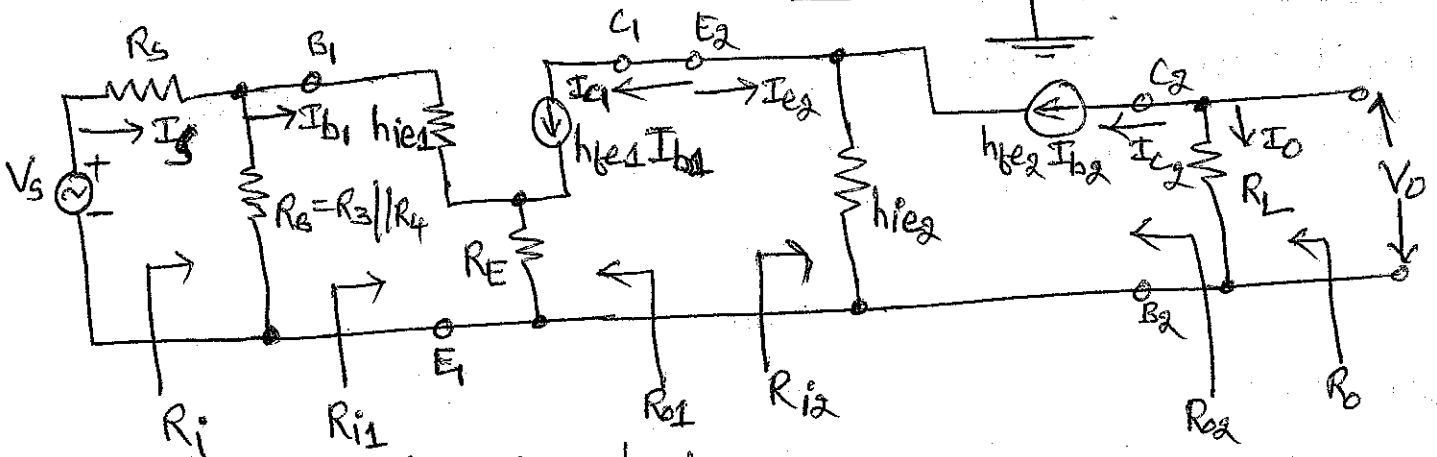
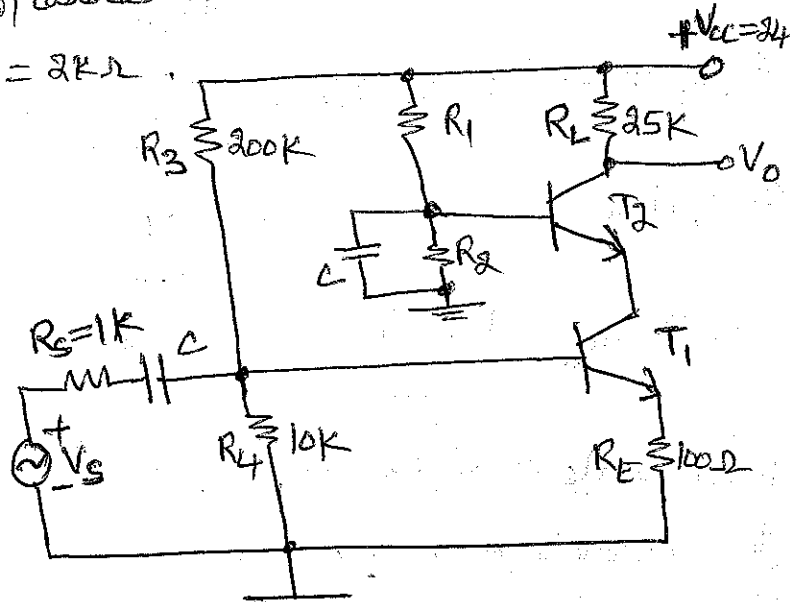
$$\therefore A_{15} = -1 \times -0.98 \times -1 \times [-50] \times 0.896 = -43.9$$

① output resistance ( $R_o$ ):

$$R_{o1} = \infty, R_{o2} = \infty, R_o = R_{o2} \parallel R_L = \infty \parallel 3K = 3K$$

Prob 2: Calculate  $A_i, R_i, A_v, A_{v_s}$  &  $R_o$  for Cascode circuit shown in figure. Assume  $h_{fe} = 100, h_{ie} = 2K\Omega$ .

soln:



Second stage (CB amplifier) analysis:

① Current gain  $A_{i2} = \frac{h_{fe}}{1+h_{fe}} = \frac{100}{1+100} = 0.99$

② Input resistance  $R_{i2} = \frac{h_{ie}}{1+h_{fe}} = \frac{2K}{1+100} = 19.8\Omega$

③ Voltage gain  $A_{v2} = \frac{A_{i2} \cdot R_{L2}}{R_{i2}} = \frac{0.99 \times 25K \times 10^3}{19.8} = 1250$

First stage analysis (CE amplifier with unbypassed  $R_E$ ):

④ Current gain  $A_{i1} = -h_{fe} = -100$

⑤ Input resistance  $R_{i1} = h_{ie} + (1+h_{fe})R_E = 2k + (1+100) \times 100 = 12.1k$

⑥ Voltage gain  $A_{V1} = \frac{A_{i1} \times R_{L1}}{R_{i1}} = \frac{-100 \times 19.2}{12.1k} = -0.1636$   $\left\{ \because R_{L1} = R_{i2} \right\}$

⑦ overall voltage gain  $A_V = A_{V1} \cdot A_{V2} = -0.1636 \times 1250 = -204.5$

⑧ overall input resistance  $R_i = R_{i1} \parallel R_B = 12.1k \parallel 9.523k = 5.323k$

$R_B = R_3 \parallel R_4 = 200k \parallel 100k$   
 $R_B = 9.523k$

⑨ Voltage gain  $A_{Vs} = A_V \cdot \frac{R_i}{R_i + R_s} = \frac{V_o}{V_s} = -204.5 \times \frac{5.323k}{5.323k + 1k}$

$A_{Vs} = -172.18$

⑩ Current gain  $A_i = \frac{I_o}{I_s} = \frac{I_o}{I_{e2}} \times \frac{I_{e2}}{I_{e1}} \times \frac{I_{e1}}{I_{b1}} \times \frac{I_{b1}}{I_s}$

$\frac{I_o}{I_{e2}} = -1, \frac{I_{e2}}{I_{e1}} = -A_{i2}, \frac{I_{e1}}{I_{b1}} = -1, \frac{I_{b1}}{I_s} = \frac{R_B}{R_B + R_{i1}}$

$\therefore A_i = -1 \times -A_{i2} \times -1 \times -A_{i1} \times \frac{R_B}{R_B + R_{i1}}$

$= -1 \times (-0.99) \times -1 \times (-100) \times \frac{9.523k}{9.523k + 12.1k} = -43.6$

⑪ output resistance ( $R_o$ ):

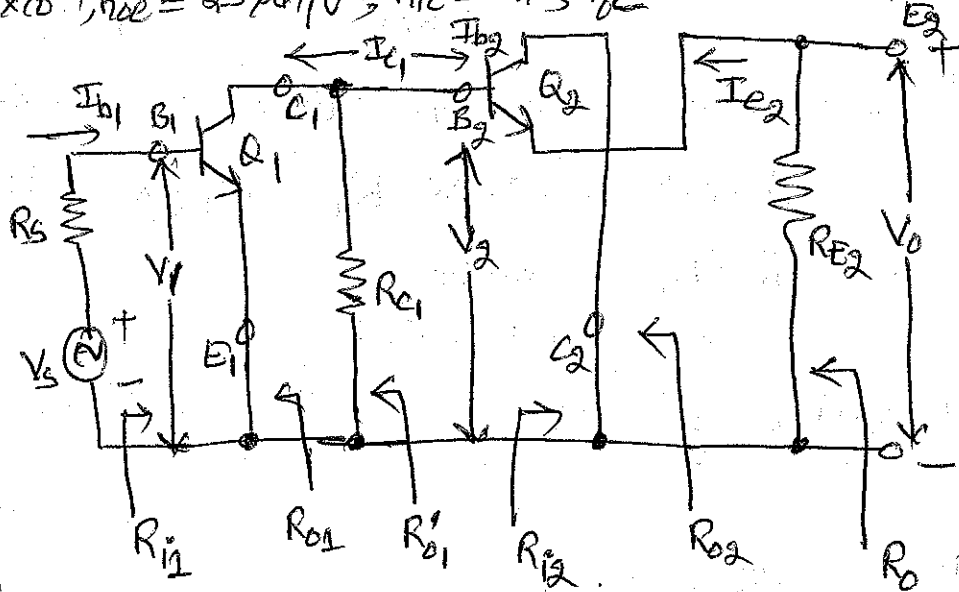
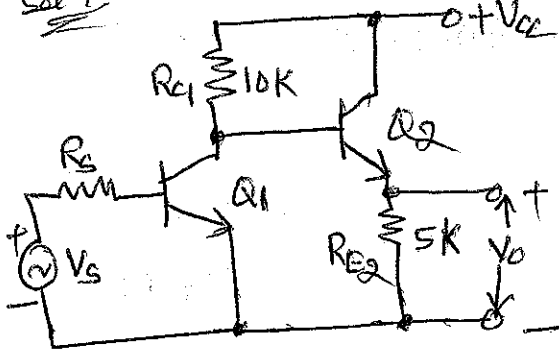
$R_{o1} = \infty, R_{o2} = \infty, R_o = R_{o2} \parallel R_L = \infty \parallel 25k = 25k$

## CE-CC Amplifiers:

Prob 1: A two stage CE-CC amplifier is shown in figure. Calculate  $A_v$ ,  $A_i$ ,  $R_i$ ,  $R_o$ ,  $A_{i2}$  &  $A_{v2}$

if  $h_{ie} = 2k$ ,  $h_{fe} = 50$ ,  $h_{re} = 6 \times 10^{-4}$ ,  $h_{oe} = 25 \mu A/V$ ,  $h_{ic} = 2k$ ,  $h_{fc} = -56$ ,  $h_{rc} = 1$  and  $h_{oc} = 25 \mu A/V$ .

Sol 1:



### Second stage analysis (CC amplifier):

$$h_{oc} \cdot R_{L2} = h_{oc} \cdot R_{E2} = 25 \times 10^{-6} \times 5 \times 10^3 = 0.125 > 0.1 \text{ so use exact analysis}$$

$$\textcircled{1} \text{ Current gain } A_{i2} = \frac{-I_{e2}}{I_{b2}} = \frac{-h_{fc}}{1 + h_{oc} \cdot R_{E2}} = \frac{-(-51)}{1 + 25 \times 10^{-6} \times 5 \times 10^3} = 45.3$$

$$\textcircled{2} \text{ Input resistance } R_{i2} = h_{ic} + h_{rc} A_{i2} R_{E2} = 2 \times 10^3 + 1 \times 45.3 \times 5 \times 10^3$$

$$R_{i2} = 228.5 k\Omega$$

$$\textcircled{3} \text{ Voltage gain } A_{v2} = \frac{V_o}{V_2} = \frac{A_{i2} \times R_{E2}}{R_{i2}} = \frac{45.3 \times 5 \times 10^3}{228.5 \times 10^3} = 0.991$$

### First stage analysis (CE amplifier):

$$R_{L1} = R_{C1} \parallel R_{i2} = 10k \parallel 228.5k = 9.52 k\Omega$$

$$h_{oc} \cdot R_{L1} = 25 \times 10^{-6} \times 9.52 \times 10^3 = 0.239 > 0.1 \text{ so use exact analysis}$$

$$\textcircled{4} \text{ Current gain } A_{i1} = \frac{-I_{c1}}{I_{b1}} = \frac{-h_{fc}}{1 + h_{oc} \cdot R_{L1}} = \frac{-50}{1 + 25 \times 10^{-6} \times 9.52 \times 10^3}$$

$$A_{i1} = -40.34$$

$$\textcircled{5} \text{ Input resistance } (R_{i1}) = h_{ie} + h_{re} A_{i1} \cdot R_{L1}$$

$$= 2 \times 10^3 - 6 \times 10^{-4} \times 40.34 \times 9.52 \times 10^3$$

$$R_{i1} = 1.768 k\Omega$$

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⑥ Voltage gain  $A_{V1} = \frac{V_2}{V_1} = \frac{A_{i1} R_{L1}}{R_{i1}} = \frac{-40.34 \times 9.52 \times 10^3}{1.768 \times 10^3} = -218$

⑦ output resistance ( $R_o$ ):

$$Y_{o1} = h_{oe} - \frac{h_{fe} \cdot h_{re}}{h_{ie} + R_s} = 25 \times 10^{-6} - \frac{50 \times 6 \times 10^{-4}}{2 \times 10^3 + 1 \times 10^3} = 1.5 \times 10^{-5} \text{ A/V}$$

$$\therefore R_{o1} = \frac{1}{Y_{o1}} = 66.7 \text{ k}\Omega$$

$$R_{o1}' = R_{e1} \parallel R_{o1} = 10 \text{ k} \parallel 66.7 \text{ k} = 8.69 \text{ k}\Omega$$

$$Y_{o2} = h_{oc} - \frac{h_{bc} \cdot h_{rc}}{h_{ic} + R_{s2}} \quad \text{where } R_{s2} = R_{o1}'$$

$$Y_{o2} = 25 \times 10^{-6} - \frac{-51 \times 1}{2 \times 10^3 + 8.69 \times 10^3} = 4.79 \text{ mA/V}$$

$$\therefore R_{o2} = \frac{1}{Y_{o2}} = 208 \Omega$$

$$\therefore R_o = R_{o2} \parallel R_{E2} = 208 \parallel 5 \text{ k} = 199.69 \Omega$$

⑧ overall voltage gain  $A_V = \frac{V_o}{V_i} = \frac{V_o}{V_2} \cdot \frac{V_2}{V_1} = A_{V2} \cdot A_{V1} = 0.991 \times (-218.5)$   
 $A_V = -216.5$

⑨ Voltage gain  $A_{Vs} = \frac{V_o}{V_s} = A_V \cdot \frac{R_{i1}}{R_{i1} + R_s} = -216.5 \times \frac{1.768 \text{ k}}{1.768 \text{ k} + 1 \text{ k}}$   
 $A_{Vs} = -138.28$

⑩ overall current gain ( $A_i$ )

$$A_i = \frac{-I_{e3}}{I_{b1}} = \frac{-I_{e2}}{I_{b2}} \times \frac{I_{b2}}{I_{e1}} \times \frac{I_{e1}}{I_{b1}}$$

$$\frac{-I_{e2}}{I_{b2}} = A_{i2} ; \frac{+I_{e1}}{I_{b1}} = -A_{i1} ; \frac{I_{b2}}{I_{e1}} = \frac{-R_{c1}}{R_{i2} + R_{c1}} = \frac{-10 \text{ k}}{220.5 \text{ k} + 10 \text{ k}} = -0.0419$$

$$\therefore A_i = +45.3 \times (-0.0419) \times (+40.34)$$

$$A_i = -76.56$$

2

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## Darlington Amplifier:

→ A very popular connection of two BJT's for operation as one super-beta transistor is the darlington connection.

→ The main feature of the darlington connection is that the composite transistor act as a single unit with a current gain that is product of the current gains of the individual transistors.

→ If the connection is made using two separate transistors having current gain of  $\beta_1$  and  $\beta_2$ , the darlington connection provides a current gain of  $\beta_D = \beta_1 \cdot \beta_2$ .

→ If the two transistors are matched such that  $\beta_1 = \beta_2 = \beta$ , the darlington connection provides a current gain of  $\beta_D = \beta^2$ .

→ when two transistors having high current gain are connected as a darlington pair, the overall gain of the pair becomes very high.

→ Darlington pairs are generally available in IC packages. The package has only three terminals namely, base, emitter and collector, it can be considered as a single darlington transistor having very high current gain as compared to other typical single transistor.

→ Darlington transistor is commonly used in emitter follower circuit. This gives an equivalent circuit of two emitter followers in cascade, thereby increasing the input impedance.

### Biasing the darlington circuit:

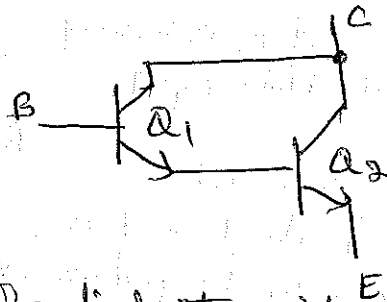
$$I_B = \frac{V_{CC} - V_{BE}}{R_B + \beta_D R_E}$$

as  $I_E = (\beta_D + 1) I_B$

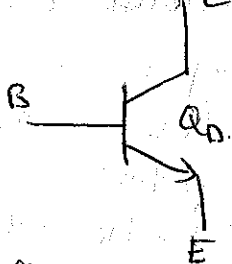
$$I_E \approx \beta_D I_B$$

$$V_E = I_E R_E$$

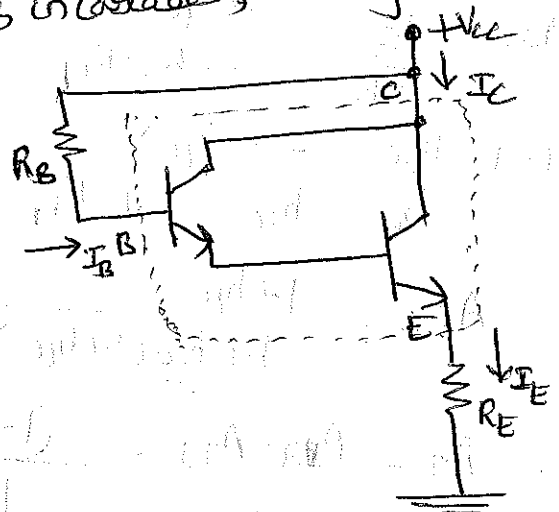
$$V_B = V_E + V_{BE}$$



(A) Darlington transistor connection.



(B) Single darlington transistor.



Handwritten notes and calculations at the bottom of the page, including the derivation of the input impedance  $Z_{in}$  for the Darlington emitter follower circuit. The notes show that  $Z_{in} = \beta_D R_E + (\beta_D + 1) R_B$ .

## Darlington Composite Emitter Follower:

→ For some applications, it is necessary to have an amplifier with high input impedance.

→ Emitter followers may be used to have input resistances of about  $500k\Omega$ . For achieving still higher input impedances, the Darlington connection shown in figure is used.

→ Darlington connection has two transistors forming a composite pair. The input resistance of the second transistor constitutes the emitter load for the first.

→ The Darlington circuit consists of two cascaded emitter followers with infinite emitter resistance in the first stage.

→ Assume  $h_{oe}R_e \leq 0.1$  and  $h_{fe}R_e \gg h_{ie}$ , so use approximate analysis for second stage.  $R_{i2} = h_{ie} + (1+h_{fe})R_e \approx (1+h_{fe})R_e$   $\left\{ \because R_{L2} = R_e \right\}$

$$A_{I1} = \frac{I_o}{I_b} = \frac{I_o}{I_2} \cdot \frac{I_2}{I_b} = A_{I2} \cdot A_{I1}$$

$$A_{I2} = \frac{I_o}{I_2} = (1+h_{fe}) \quad \left\{ \because \text{Approximate analysis of CC } \right. \\ \left. \text{Second stage} \right\}$$

$$A_{I1} = \frac{I_2}{I_b} = \frac{-h_{fc}}{1+h_{oc}R_L} \quad \left\{ \because \text{Exact analysis of CC first stage} \right. \\ \left. \text{as load of } Q_1 \text{ is } R_{i2}. \right\} \\ \text{So } h_{oc}R_{i2} \neq 0.1$$

But  $h_{fc} = -(1+h_{fe})$   
 $h_{oc} = h_{oe}$  and  $R_L = R_{i2} \approx (1+h_{fe})R_e$ .

$$\therefore A_{I1} = \frac{1+h_{fe}}{1+h_{oe}(1+h_{fe})R_e} \approx \frac{1+h_{fe}}{1+h_{oe}h_{fe}R_e}$$

$$\therefore A_I = A_{I2} \cdot A_{I1} = \frac{(1+h_{fe})^2}{1+h_{oe}h_{fe}R_e}$$

Input resistance for  $Q_1$  is,

$$R_{i1} = h_{ic} + h_{oc} \cdot A_{I1} R_{L1} \approx A_{I1} \cdot R_{L1}$$

But  $h_{ic} = h_{ie}$ ,  $h_{oc} = 1$ ,  $R_{L1} = R_{i2}$

$$\therefore R_{i1} = h_{ie} + \frac{(1+h_{fe})^2}{1+h_{oe}h_{fe}R_e} \times (1+h_{fe})R_e \approx \frac{(1+h_{fe})^2 R_e}{1+h_{oe}h_{fe}R_e}$$

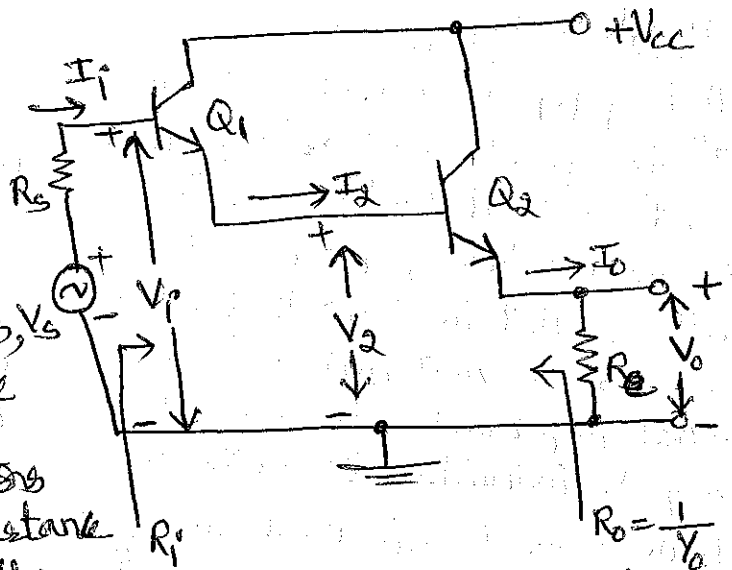


Fig: Darlington Composite Emitter follower



$$A_{v2} = 1 - \frac{h_{ie}}{R_{i2}}$$

$$A_{v1} = 1 - \frac{h_{ie}}{R_{i2}} \quad \text{But } R_{i2} = h_{ie} + A_{v1} R_{i2} \approx A_{v1} R_{i2}$$

$$A_{v1} = 1 - \frac{h_{ie}}{A_{v1} R_{i2}}$$

$$\therefore A_v = A_{v1} \cdot A_{v2} = \left(1 - \frac{h_{ie}}{A_{v1} R_{i2}}\right) \left(1 - \frac{h_{ie}}{R_{i2}}\right)$$

$$A_v = 1 - \frac{h_{ie}}{R_{i2}} - \frac{h_{ie}}{A_{v1} R_{i2}} + \frac{h_{ie}^2}{A_{v1} R_{i2}^2}$$

As  $A_{v1} \gg 1$  so neglecting the 3rd & 4th terms we get,

$$A_v \approx 1 - \frac{h_{ie}}{R_{i2}}$$

The output resistance  $R_{o1}$  of Q1 is,

$$R_{o1} = \frac{R_s + h_{ie}}{1 + h_{fe}}$$

$$V_{o1} = h_{oc} - \frac{h_{fc} R_{oc}}{h_{ie} + R_s} \quad \text{But } \begin{matrix} h_{oc} = h_{oe} \\ h_{ic} = h_{ie} \\ h_{oc} = 1 \\ h_{fc} = -(1+h_{fe}) \end{matrix}$$

$$\therefore V_{o1} = h_{oe} + \frac{(1+h_{fe})}{h_{ie} + R_s}$$

$$V_{o1} \approx \frac{(1+h_{fe})}{h_{ie} + R_s}$$

Now  $R_{o1}$  acts as source resistance for second stage so output resistance of second stage is,

$$R_{o2} = \frac{R_{o1} + h_{ie}}{1 + h_{fe}}$$

$$R_{o2} = \frac{R_s + h_{ie}}{1 + h_{fe}} + h_{ie}$$

$$R_{o2} = \frac{R_s + h_{ie}}{(1 + h_{fe})^2} + \frac{h_{ie}}{1 + h_{fe}}$$

→ Hence the Darlington emitter follower has higher current gain, a higher input resistance, a voltage gain less close to unity and a lower output resistance than a single-stage emitter follower.

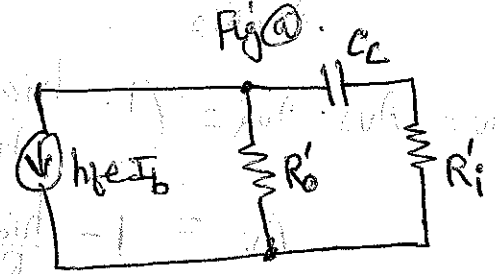
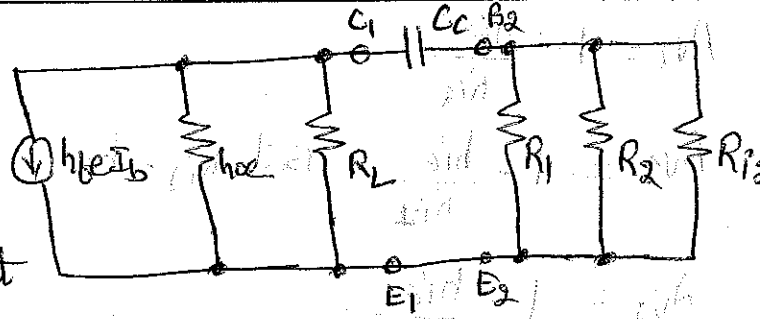
→ The drawback of Darlington transistor pair is that the leakage current of the transistor Q1 is amplified by the transistor Q2 and hence the overall leakage current may be high so Darlington connection of three or more transistors is not used.

## Analysis of RC Coupled Amplifiers:

→ Assume  $C_E$  is large enough to provide short circuit for the entire audio frequency range.

→ Fig (a) shows h-parameter equivalent circuit for output section of first stage and the input section of second stage.

$$R_o' = \frac{1}{h_{oe}} \parallel R_L \quad \text{and} \quad R_i' = R_{i1} \parallel R_{i2} \parallel R_{i3}$$



### ① Mid frequency response:

→ At mid frequencies the impedance offered by coupling capacitance  $C_c$  is so small such that it acts as an effective short circuit.

$$V_o = \frac{-h_{fe} I_b R_o' R_i'}{R_o' + R_i'}$$

$$\frac{V_o}{V_i} = A_{(mid)} = \frac{-h_{fe} I_b R_o' R_i'}{(R_o' + R_i') V_i}$$

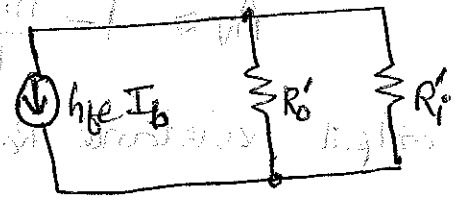


Fig (c)

### ② Low frequency response:

→ In this frequency range the impedance offered by coupling capacitor is comparable to the load resistance so that coupling capacitor largely affects the amplification. Therefore we include the capacitor in this equivalent circuit.

$$X_c = \frac{1}{2\pi f C_c}$$

$$V_o = \frac{-h_{fe} I_b R_o' R_i'}{R_o' + R_i' + \frac{1}{j\omega C_c}}$$

$$A_{(low)} = \frac{V_o}{V_i} = \frac{-h_{fe} I_b R_o' R_i'}{(R_o' + R_i' + \frac{1}{j\omega C_c}) V_i}$$

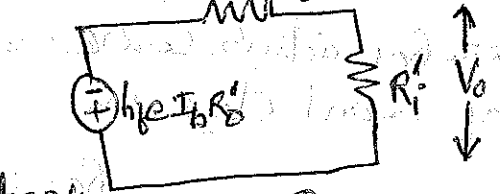


Fig (d)

$$A_{v(\text{low})} = \frac{-h_{fe} R_o' R_i' I_b}{R_o' + R_i'} \times \frac{1}{V_i} \times \frac{1}{1 + \frac{1}{j\omega C_c (R_o' + R_i')}}}$$

$$A_{v(\text{low})} = \frac{A_{v(\text{mid})}}{1 - \frac{j}{\omega C_c (R_o' + R_i')}}}$$

$$\therefore \frac{A_{v(\text{low})}}{A_{v(\text{mid})}} = \frac{1}{1 - \frac{j}{\omega C_c (R_o' + R_i')}}}$$

Let  $f_L = \frac{1}{2\pi C_c (R_o' + R_i')}$

$$\therefore \frac{A_{v(\text{low})}}{A_{v(\text{mid})}} = \frac{1}{1 - j(f_L/f)}$$

$$\Rightarrow \left| \frac{A_{v(\text{low})}}{A_{v(\text{mid})}} \right| = \frac{1}{\sqrt{1 + (f_L/f)^2}}$$

At  $f = f_L$   $\frac{A_{v(\text{low})}}{A_{v(\text{mid})}} = \frac{1}{\sqrt{2}} = 0.707$

Hence the output power at low frequency will be half of the signal power at mid frequency range.

③ High frequency response:

→ In high frequency range the reactance offered by  $C_c$  is very small and hence can be considered as short circuited, but the shunting capacitors provide low reactance which is in parallel with output reducing the gain.

By similar analysis we get,

$$\frac{A_{v(\text{high})}}{A_{v(\text{mid})}} = \frac{1}{\sqrt{1 + (f/f_H)^2}} \quad \text{and at } f = f_H \quad \frac{A_{v(\text{high})}}{A_{v(\text{mid})}} = \frac{1}{\sqrt{2}} = 0.707$$

Prob 1: A Coupling Capacitor is used between two stages of an amplifier which uses BJT connected in CE configuration where  $h_{fe} = 100$ ,  $h_{ie} = 2k\Omega$ ,  $R_L = 3k\Omega$ ,  $R_1 = 47k\Omega$ ,  $R_2 = 4.7k\Omega$  and  $C_c = 5\mu F$ . Calculate lower 3dB frequency  $f_L$  and calculate the frequency at which voltage gain is down by 12dB from its mid frequency value. use approximate analysis.

Soln:  $R_o' = \frac{1}{h_{oe}} \parallel R_L \approx R_L$  as  $\frac{1}{h_{oe}} \gg R_L$

$R_o' = 3k\Omega$

$R_i' = R_1 \parallel R_2 \parallel R_{i2} = R_1 \parallel R_2 \parallel h_{ie}$  }  $R_{i2} = h_{ie}$

$R_i' = 47k \parallel 4.7k \parallel 2k = 1.36k\Omega$

$\therefore f_L = \frac{1}{2\pi C_c (R_o' + R_i')} = \frac{1}{2\pi \times 5 \times 10^{-6} (3 \times 10^3 + 1.36 \times 10^3)} = 7.3 \text{ Hz}$

It is given that,

$20 \log \left| \frac{A_v(\text{low})}{A_v(\text{mid})} \right| = -12$

$\therefore \left| \frac{A_v(\text{low})}{A_v(\text{mid})} \right| = \frac{1}{\sqrt{1 + \left(\frac{f_L}{f}\right)^2}} \approx 0.251$

$\Rightarrow \left(\frac{1}{0.251}\right)^2 = 1 + \left(\frac{f_L}{f}\right)^2$

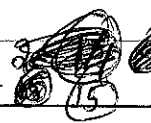
$\Rightarrow 15.87 = 1 + \left(\frac{f_L}{f}\right)^2$

$\Rightarrow f = \frac{f_L}{\sqrt{14.87}} = 1.893 \text{ Hz}$

Therefore voltage gain is down by 12dB from its mid frequency value at frequency 1.893 Hz.

$f_L = \frac{1}{2\pi C_c (R_o' + R_i')}$

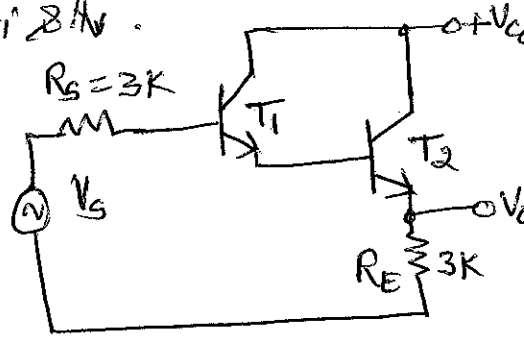
(problem on darlington pair)

2- 

prob 1: For circuit shown in figure calculate  $R_i$ ,  $R_o$ ,  $A_i$  &  $A_v$ .

$h_{ie} = 1.1K\Omega$ ,  $h_{fe} = 50$ ,  $h_{re} = 2.5 \times 10^{-4}$ ,  $h_{oe} = 25\mu A/V$ .

Sol 1:  $h_{oe} \cdot R_{L2} = 25 \times 10^{-6} \times 3 \times 10^3$   $\left\{ \begin{array}{l} R_{L2} = R_{E2} \\ < 0.1 \text{ so use approximate analysis} \end{array} \right.$



$A_{i2} = 1 + h_{fe} = 1 + 50 = 51$

$R_{i2} = h_{ie} + (1 + h_{fe}) R_{L2} = 1.1 \times 10^3 + (1 + 50) \times 3 \times 10^3 = 154.1K\Omega$

$A_{v2} = 1 - \frac{h_{ie}}{R_{i2}} = 1 - \frac{1.1 \times 10^3}{154.1K\Omega} = 0.9928$

$h_{oe} \cdot R_{L1} = h_{oe} \cdot R_{i2} = 25 \times 10^{-6} \times 154.1K\Omega = 3.85 > 0.1$  so use exact analysis

$A_{i1} = \frac{1 + h_{fe}}{1 + h_{oe}(1 + h_{fe})R_E} = \frac{1 + 50}{1 + 25 \times 10^{-6}(1 + 50) \times 3 \times 10^3} = 10.56$

$R_{i1} = h_{ie} + A_{i1} R_{L1} = 1.1 \times 10^3 + 10.56 \times 154.1 \times 10^3 = 1.628M\Omega$

$A_{v1} = 1 - \frac{h_{ie}}{R_{i1}} = 1 - \frac{1.1 \times 10^3}{1.628 \times 10^6} = 0.999$

$A_v = A_{v1} \cdot A_{v2} = 0.9918$  (2)  ~~$A_v \approx 1 - \frac{h_{ie}}{R_{i2}} = 0.9928$~~

$A_I = A_{I1} \cdot A_{I2} = 10.56 \times 51 = 538.56$

(a)  $A_I = \frac{(1 + h_{fe})^2}{1 + h_{oe}(1 + h_{fe})R_E} = \frac{(1 + 50)^2}{1 + 25 \times 10^{-6}(1 + 50) \times 3 \times 10^3} = 539.06$

$R_{o1} = \frac{h_{ie} + R_s}{1 + h_{fe}} = \frac{1.1 \times 10^3 + 3 \times 10^3}{1 + 50} = 80.39\Omega$

$R_{o2} = \frac{h_{ie} + R_{s2}}{1 + h_{fe}} = \frac{h_{ie} + R_{o1}}{1 + h_{fe}} = \frac{1.1 \times 10^3 + 80.39}{1 + 50} = 23.145\Omega$

$R_o = R_{o2} \parallel R_E = 23.145 \parallel 3 \times 10^3 = 22.97\Omega$



Direct Coupled (DC) Amplifiers:

- In the field of instrumentation and power supplies there are many signals that change very slowly with time.
- To process these signals, circuits must be employed whose frequency response is stretched flat down to DC.
- This prevents the use of interstage coupling elements such as capacitors and transformers as these components attenuate very low frequencies and completely block DC signals.
- There are two basic techniques for amplifying such low frequency signals that change very slowly with time.
- One is to use direct coupled (DC) amplifiers and the second one requires chopping the dc signals so as to change it to an ac signal which is then amplified using conventional AC amplifiers and reconstructed at the output as dc.

→ In the design of DC amplifiers one should ensure that dc levels of each stage are compatible with those of other circuits to which the stage is connected.

→ As an example, consider the identical amplifier stages in figure (a).  
 $V_{CC1} = V_{CC2} = 12V$ ,  $V_{B1} = V_{B2} = 2V$ ,  
 $V_{E1} = V_{E2} = 1.5V$  and  $V_{C1} = V_{C2} = 5V$ .

Each stage is biased at  $V_{BE} = 0.5V$  and  $V_{CE} = 3V$  and also there is a potential difference of  $3V$  between the collector of  $Q_1$  and the base of  $Q_2$ .

→ For ac operation, a capacitor is connected between the collector of  $Q_1$  and the base of  $Q_2$  as in figure (b).

→ By this method, the ac signal is coupled from  $Q_1$  to  $Q_2$  but the capacitor charges to  $3V$  dc so that  $V_{CE1}$  is still at  $5V$  and  $V_{B2}$  is still at  $2V$ . The dc levels of both the stages remain independent of the other.

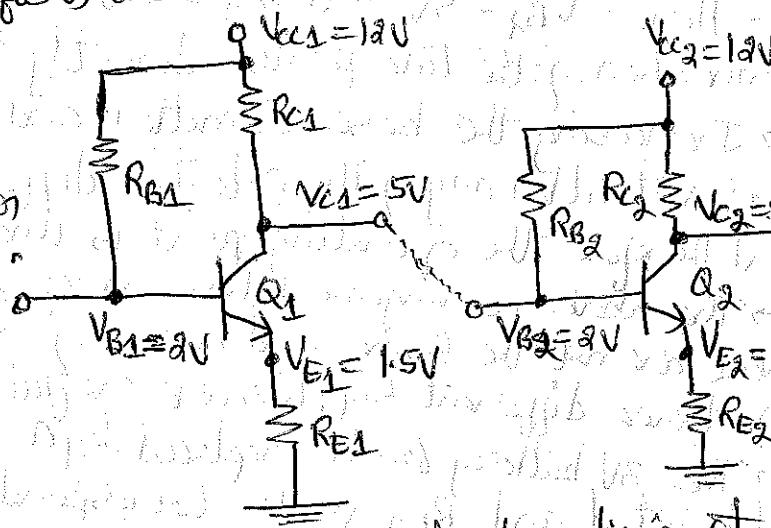


Fig (a): Two identical amplifier stages.

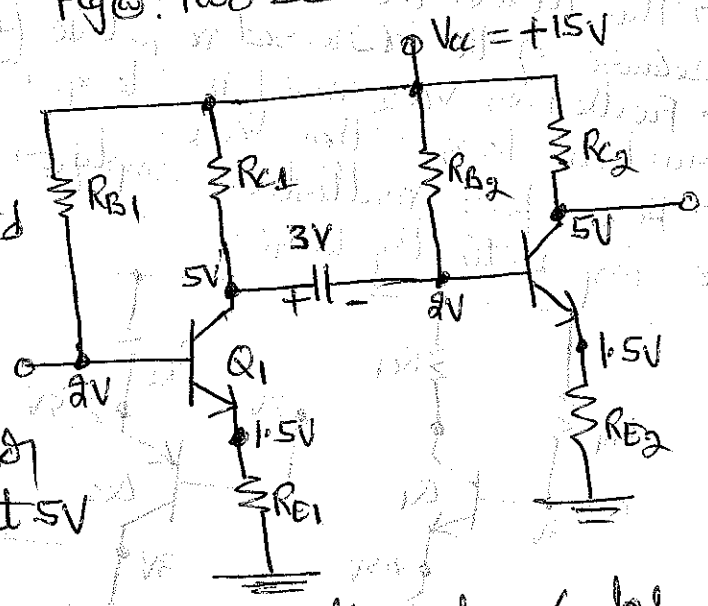


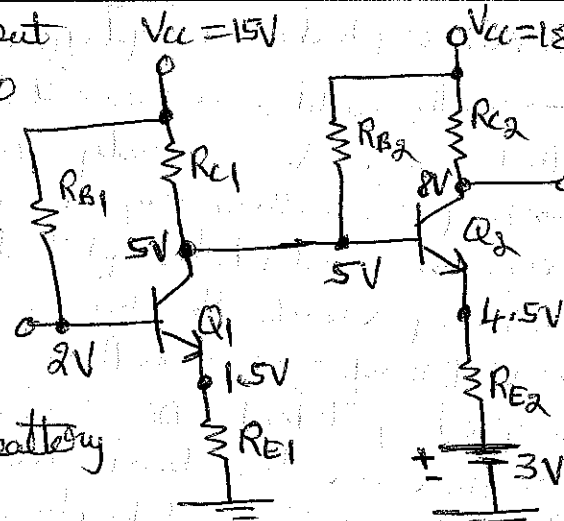
Fig (b): Two amplifier stages coupled by a capacitor.

amplifier stages with A: DPT

→ For DC operation, the capacitor is to be omitted but the collector of  $Q_1$  cannot be directly connected to the base of  $Q_2$  unless the voltages at these points are the same.

→ one possible solution is to leave the first stage as it is but lift the second stage by 3V relative to ground so that  $V_{B2}$ ,  $V_{E2}$  and  $V_{C2}$  are all 3V higher than they were earlier.

→ This may be accomplished by connecting a 3V battery in series with  $R_{E2}$  and using a 18V supply for  $V_{CC}$  as shown in figure (c).



Fig(c): A two stage DC amplifier

→ Here  $V_{B2} = 5V$  and  $V_{C2} = 8V$ . This causes  $V_{C1}$  to be equal to  $V_{B2}$  enabling connection of the two points directly to each other.

→ Increasing the base, emitter and collector voltages by the same amount does not alter any of the potential differences i.e.  $V_{BE2} = 0.5V$  and  $V_{CB2} = 3V$  and therefore the operating point is unchanged.

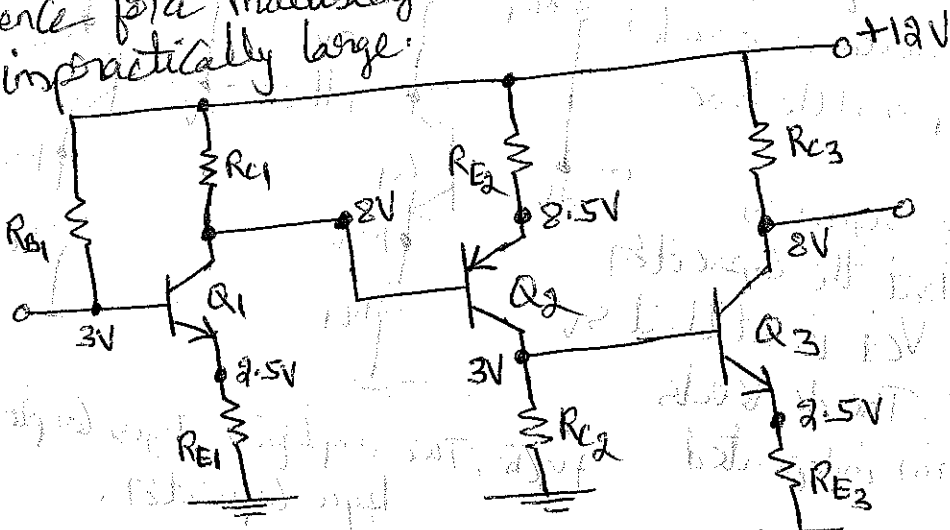
→ The above arrangement has a no. of obvious disadvantages. As  $V_{CC1}$  and  $V_{CC2}$  are not the same and because of 3V battery in series with  $R_{E2}$  a total of three different supplies are required.

→ The 3V battery can be replaced by a 3V zener diode or it could be simply eliminated and  $R_{E2}$  made correspondingly larger.

→ This would increase the input resistance of  $Q_2$  and lower the gain because of the increased negative feedback.

→ Further as  $V_{CC2}$  must be larger than  $V_{CC1}$  if a third stage is added  $V_{CC3}$  must be larger than  $V_{CC2}$ .

→ Hence for a multistage amplifier the required DC voltage supplies might be impractically large.



Fig(d): A three stage DC amplifier



- A circuit arrangement that solves the above problem is shown in fig ①. Here alternate polarity transistors are cascaded and the dc voltages are so adjusted that each of the three transistors is operating at exactly the same point.
- In this circuit there is a 0.5V forward bias across each base-emitter junction and 5V reverse bias across each collector-base junction. Further, it is to be noted that only one external supply is needed.
- An additional problem peculiar to DC amplifiers is that small changes in the operating point due to temperature or power supply fluctuations as well as aging of circuit components are also amplified as there is nothing to block dc and these changes appear in the amplified form across the output.
- The dc input voltage required to bring the output voltage back to its original level (no signal level) is a measure of performance of DC amplifiers and is called Voltage offset  $V_{os}$ .
- Similarly a dc input current known as offset current  $I_{os}$  might be required to bring the output current back to its original level.
- Both the offset voltage and current tend to vary with time and temperature.
- DC amplifiers generally require a potentiometer adjustment for cancelling such offsets.
- The manufacturer also usually specify the values of  $E_{os}$  and  $I_{os}$  and the expected drift with time and temperature.
- Stabilising techniques can also be applied here.

A circuit is composed of various parts. The most important part is the power source, which provides the energy to drive the current. The circuit is completed by the load, which converts the electrical energy into another form, such as heat or light. The connecting wires provide a path for the current to flow. The circuit is controlled by switches, which can open or close the circuit. The current flows from the positive terminal of the power source, through the load, and back to the negative terminal. The amount of current that flows depends on the resistance of the load and the voltage of the power source. The power source is usually a battery or a generator. The load can be a resistor, a lamp, or a motor. The connecting wires are usually made of copper or aluminum. The switches are usually made of plastic and metal. The circuit is a closed loop, and the current flows continuously as long as the power source is connected and the circuit is closed.